

main.tex

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```

1 \documentclass[xcolor=dvipsnames]{beamer}
2 \usepackage[utf8]{inputenc}
3 \usepackage{xcolor}
4 \title{\textcolor{blue}{Assignment 2}}
5 \author{Anita}
6 College Rollno. MAT/20/55\University Roll no. 20044563008}
7 \institute{\large{Mata Sundri College for Women\University of Delhi}}
8 \date{}
9 \usepackage{graphicx}
10 \settheme{Madrid}
11 \definecolor{UBCblue}{rgb}{1,2}
12 \setbeamercolor{frametitle}{bg=green!40!black}
13 \usecolortheme[named=UBCblue]{structure}
14 \begin{document}
15 \frame{\titlepage}
16 \begin{frame}{Copy point 1 on page number 69}
17 \begin{block}{part-1}
18 \begin{itemize}
19 \item Let  $\mathbf{x}=(x_1, \dots, x_n)$ ,
20 where the  $x_i$  are non-negative real numbers.
21 Set
22 \[
23 M_r(\mathbf{x}) = \left(\frac{x_1^r+x_2^r
24 +\dots+x_n^r}{n}\right)^{1/r},
25 \; ; \; r \in \mathbf{R} \setminus \{0\},
26 \]
27 and
28 \[
29 M_0(\mathbf{x}) = \left(x_1 x_2 \dots x_n\right)^{1/n}
30 \] We call  $M_r(\mathbf{x})$  the  $r$ th power mean
31 of  $\mathbf{x}$ .
32
33 Claim:
34 \[
35 \lim_{r \rightarrow 0} M_r(\mathbf{x}) =
36 M_0(\mathbf{x}).
37 \]
38 \end{itemize}
39 \end{block}
40 \end{frame}

```

File outline

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41 \begin{frame}{copy point 2 on page 69}
42 \begin{block}{part-2}
43 \begin{itemize}
44 \item
45   Define
46   \[
47   V_n=
48   \left[
49 \begin{array}{cccc}
50   1 & 1 & 1 & 1 & \dots & & 1 \\
51   x_1 & x_2 & x_3 & \dots & x_n \\
52   x_1^2 & x_2^2 & x_3^2 & \dots & x_n^2 \\
53   \vdots & \vdots & \vdots & \ddots & \vdots \\
54   x_1^{n-1} & x_2^{n-1} & x_3^{n-1} & \dots & x_n^{n-1}
55 \end{array}
56 \right] .
57 \]
58 We call  $V_n$  the Vander monde matrix of order  $n$ .
59
60 Claim:
61 \[
62 \det V_n = \prod_{1 \leq i < j \leq n} (x_j - x_i).
63 \]
64 \end{itemize}
65 \end{block}
66
67 \end{frame}
68
69 \begin{frame}{Questions 4}
70 \begin{block}{4.1}
71    $3^3+4^3+5^3 = 6^3$ 
72 \end{block}
73 \begin{block}{4.2}
74    $\sqrt{100}=10$ 
75 \end{block}
76 \begin{block}{4.3}
77    $(a+b)^3 = a^3+b^3+3ab^2+3ba^2$ 
78 \end{block}
79 \end{frame}
80 \begin{frame}{remaining parts of question 4}

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81 - \begin{block}{4.4}
82 - $\sum_{k=1}^n \{\frac{n(n+1)}{2}\}$
83 - \label{sum}$\\
84 - \end{block}
85 - \begin{block}{4.5}
86 - $\frac{\pi}{4} = 1-\frac{1}{3}+\frac{1}{5}-\frac{1}{7}+\frac{1}{9}-\frac{1}{11}+\dots$\\
87 - \end{block}
88 - \begin{block}{4.6}
89 - $\cos{\theta}=\sin{(90^\circ-\theta)}$\\
90 - \end{block}
91 - \begin{block}{4.7}
92 - $e^{i\theta} = \cos(\theta)+i \sin(\theta)$\\
93 - \end{block}
94 - \end{frame}
95 - \begin{frame}{remaining parts of question 4}
96 - \begin{block}{4.8}
97 - $\lim_{\theta \to 0} \frac{\sin(\theta)}{\theta}=1$\\
98 - \end{block}
99 - \begin{block}{4.9}
100 - $\lim_{x \to \infty} \frac{\pi \mathbf{(x)}}{x \log x}=1$
101 - \end{block}
102 - \begin{block}{4.10}
103 - $\int_{-\infty}^{\infty} e^{-x^2} dx = \sqrt{\pi}$
104 - \label{int}$
105 - \end{block}
106 - \end{frame}
107 -
108 - \begin{frame}{Question 5.}
109 - \begin{block}{5.1}
110 - Positive numbers a,b and c are the side lengths of triangle if and only if $a+b > c$, $b+c > a$, $c+a > b$.\\
111 - \end{block}
112 - \begin{block}{5.2}
113 - The area of triangle with side length a , b , c is given by Heoren's formula:
114 - \begin{eqnarray*}
115 - A = \sqrt{(s)(s-a)(s-b)(s-c)},
116 - \end{eqnarray*} where s is the semiperimeter $\frac{a+b+c}{2}$.\\
117 - \end{block}
118 - \end{frame}
119 - \begin{frame}{remaining parts of questio 5}
120 - \begin{block}{5.3}

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120 \begin{block}{3.3}
121 The volume of a rectangular tetrahedron of edge length 1 is $\frac{\sqrt{2}}{12}$\end{block}
122 \begin{block}{5.4}
123 The quadratic equation $ax^2+bx+c=0$ has roots \
124 \begin{eqnarray*}
125 r_1,r_2=&\frac{-b\pm\sqrt{b^2 - 4ac}}{2a}.
126 \end{eqnarray*}
127 \end{block}
128 \end{frame}
129 \begin{frame}{remaining parts of question 5}
130 \begin{block}{5.5}
131 The \(\mathit{derivative}\) of a function \(\mathit{f}\), denoted \(\mathit{f}'\), is defined by
132 \begin{eqnarray*}
133 f'(x)&=&\lim_{h \to 0}\frac{f(x+h)-f(x)}{h}
134 \end{eqnarray*}
135 \end{block}
136 \begin{block}{5.6}
137 A real-valued function \(\mathit{f}\) is \(\mathit{convex}\) on an interval \(\mathit{I}\) if \[
138 f(\lambda x + (1-\lambda)y) \leq \lambda f(x) + (1-\lambda)f(y),
139 \]
140 for all \(x,y \in I\) and \(0 \leq \lambda \leq 1\).
141 \end{block}
142 \end{frame}
143 \begin{frame}{remaining parts of question 5}
144 \begin{block}{5.7}
145 The general solution to the differential equation \[
146 y''-3y'+2y=0
147 \]
148 is
149 \[
150 y= C_1e^{2x} + C_2e^x.
151 \]
152 \end{block}
153 \begin{block}{5.8}
154 The \(\mathit{Fermat number}\) $F_n$ is defined as
155 \[
156 F_n=2^{2^n}+1, n \geq 0.
157 \]
158 \end{block}
159 \end{frame}
160 \begin{frame}{Question 6}
```


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```
160 \begin{frame}{Question 6}
161 \begin{block}{6.1}
162   $\frac{d}{dx}(\frac{x}{x+1}) = \frac{1}{(x+1)^2}$\
163 \end{block}
164 \begin{block}{6.2}
165   $\lim_{x \to \infty} (1+\frac{1}{n})^n = e$\
166 \end{block}
167 \end{frame}
168 \begin{frame}{remaining parts of question 6}
169 \begin{block}{6.3}
170 \[
171   \begin{vmatrix}
172     a & b \\
173     c & d
174   \end{vmatrix}
175   =
176   ad - bc
177 \]
178 \end{block}
179 \begin{block}{6.4}
180 \[
181   R_{\theta} =
182   \left[
183   \begin{array}{cc}
184     \cos\theta & -\sin\theta \\
185     \sin\theta & \cos\theta
186   \end{array}
187   \right]
188 \]
189 \end{block}
190 \end{frame}
191 \begin{frame}{ remaining parts of question 6}
192 \begin{block}{6.5}
193 \[
194   \begin{vmatrix}
195     i & j & k \\
196     a_1 & a_2 & a_3 \\
197     b_1 & b_2 & b_3
198   \end{vmatrix}
199   =
200 \]
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```
200 i\begin{vmatrix}
201 a_2 & a_3 \\
202 b_2 & b_3 \\
203 \end{vmatrix}
204 -
205 \begin{vmatrix}
206 a_1 & a_3 \\
207 b_1 & b_3 \\
208 \end{vmatrix}j
209 -
210 \begin{vmatrix}
211 a_1 & a_2 \\
212 b_1 & b_2 \\
213 \end{vmatrix}k
214 \]
215 \end{block}
216 \begin{block}{6.6}
217 \[
218 \left[
219 \begin{array}{cc}
220 a_{11} & a_{12} \\
221 a_{21} & a_{22} \\
222 \end{array} \\
223 \right] \\
224 \left[
225 \begin{array}{cc}
226 b_{11} & b_{12} \\
227 b_{21} & b_{22} \\
228 \end{array} \\
229 \right] \\
230 = \\
231 \left[
232 \begin{array}{cc}
233 a_{11} b_{11} + a_{12} b_{21} & a_{11} b_{12} + a_{12} b_{22} \\
234 a_{21} b_{11} + a_{22} b_{21} & a_{21} b_{12} + a_{22} b_{22} \\
235 \end{array} \\
236 \right] \\
237 \]
238 \end{block}
239 \end{frame}
```

Assignment 2

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part-1

- Let $x = (x_1, \dots, x_n)$, where the x_i are non-negative real numbers. Set

$$M_r(x) = \left(\frac{x_1^r + x_2^r + \dots + x_n^r}{n} \right)^{1/r}, \quad r \in \mathbb{R} \setminus \{0\},$$

and

$$M_0(x) = (x_1 x_2 \dots x_n)^{1/n}$$

We call $M_r(x)$ the *r*th power mean of x .

Claim:

$$\lim_{r \rightarrow 0} M_r(x) = M_0(x).$$

part-2

- Define

$$V_n = \begin{bmatrix} 1 & 1 & 1 & \dots & 1 \\ x_1 & x_2 & x_3 & \dots & x_n \\ x_1^2 & x_2^2 & x_3^2 & \dots & x_n^2 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ x_1^{n-1} & x_2^{n-1} & x_3^{n-1} & \dots & x_n^{n-1} \end{bmatrix}.$$

We call V_n the *Vander monde matrix* of order n .

Claim:

$$\det V_n = \prod_{1 \leq i < j \leq n} (x_j - x_i).$$

Questions 4

4.1

$$3^3 + 4^3 + 5^3 = 6^3$$

4.2

$$\sqrt{100} = 10$$

4.3

$$(a + b)^3 = a^3 + b^3 + 3ab^2 + 3ba^2$$

remaining parts of question 4

4.4

$$\sum_{k=1}^n \frac{n(n+1)}{2}$$

4.5

$$\frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \frac{1}{11} + \dots$$

4.6

$$\cos\theta = \sin(90^\circ - \theta)$$

4.7

$$e^{i\theta} = \cos(\theta) + i\sin(\theta)$$

remaining parts of question 4

4.8

$$\lim_{\theta \rightarrow 0} \frac{\sin(\theta)}{\theta} = 1'$$

4.9

$$\lim_{x \rightarrow \infty} \frac{\pi(x)}{x/\log x} = 1$$

4.10

$$\int_{-\infty}^{\infty} e^{-x^2} dx = \sqrt{\pi}$$

Question 5.

5.1

Positive numbers a, b and c are the side lengths of triangle if and only if $a+b > c$, $b+c > a$, $c+a > b$.

5.2

The area of triangle with side length a, b, c is given by *Heoren's formula*:

$$A = \sqrt{(s)(s-a)(s-b)(s-c)},$$

where s is the semiperimeter $\frac{a+b+c}{2}$.

5.3

The volume of a rectangular tetrahedron of edge length 1 is $\frac{\sqrt{2}}{12}$

5.4

The quadratic equation $ax^2 + bx + c = 0$ has roots

$$r_1, r_2 = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}.$$

remaining parts of question 5

5.5

The *derivative* of a function f , denoted f' , is defined by

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

5.6

A real-valued function f is *convex* on an interval I if

$$f(\lambda x + (1 - \lambda)y) \leq \lambda f(x) + (1 - \lambda)f(y),$$

for all $x, y \in I$ and $0 \leq \lambda \leq 1$.

remaining parts of question 5

5.7

The general solution to the differential equation

$$y'' - 3y' + 2y = 0$$

is

$$y = C_1 e^x + C_2 e^{2x}.$$

5.8

The *Fermatnumber* F_n is defined as

$$F_n = 2^{2^n}, n \geq 0.$$

Question 6

6.1

$$\frac{d}{dx} \left(\frac{x}{x+1} \right) = \frac{1}{(x+1)^2}$$

6.2

$$\lim_{x \rightarrow \infty} \left(1 + \frac{1}{n} \right)^n = e$$

remaining parts of question 6

6.3

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$$

6.4

$$R_\theta = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix}$$

remaining parts of question 6

6.5

$$\begin{vmatrix} i & j & k \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix} = i \begin{vmatrix} a_2 & a_3 \\ b_2 & b_3 \end{vmatrix} - \begin{vmatrix} a_1 & a_3 \\ b_1 & b_3 \end{vmatrix} j - \begin{vmatrix} a_1 & a_2 \\ b_1 & b_2 \end{vmatrix} k$$

6.6

$$\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix} = \begin{bmatrix} a_{11}b_{11} + a_{12}b_{21} & a_{11}b_{12} + a_{12}b_{22} \\ a_{21}b_{11} + a_{22}b_{21} & a_{21}b_{12} + a_{22}b_{22} \end{bmatrix}$$

6.7

$$f(x) = \begin{cases} -x^2, & x < 0 \\ x^2, & 0 \leq x < 2 \\ 4, & x \geq 2 \end{cases}$$

question 7

7.1

$$1 + 2 = 3$$

$$4 + 5 + 6 = 7 + 8$$

$$9 + 10 + 11 + 12 = 13 + 14 + 15$$

$$16 + 17 + 18 + 19 + 20 = 21 + 22 + 23 + 24$$

$$25 + 26 + 27 + 28 + 29 + 30 = 31 + 32 + 33 + 34 + 35$$

7.2

$$\begin{aligned}(a + b)^2 &= (a + b)(a + b) \\ &= (a + b)a + (a + b)b \\ &= a(a + b) + b(a + b) \\ &= a^2 + ab + ba + b^2 \\ &= a^2 + ab + ab + b^2 \\ &= a^2 + 2ab + b^2\end{aligned}$$

7.3

$$\begin{aligned}
 \tan(\alpha + \beta + \gamma) &= \frac{\tan \alpha + \beta + \tan \gamma}{1 - \tan \alpha + \beta \tan \gamma} \\
 &= \frac{\frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta} + \tan \gamma}{1 - \left(\frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta}\right) \tan \gamma} \\
 &= \frac{\tan \alpha + \tan \beta + (1 - \tan \alpha \tan \beta) \tan \gamma}{1 - \tan \alpha \tan \beta - (\tan \alpha + \tan \beta) \tan \gamma} \\
 &= \frac{\tan \alpha + \tan \beta + \tan \gamma - \tan \alpha \tan \beta \tan \gamma}{1 - \tan \alpha \tan \beta - \tan \alpha \tan \gamma - \tan \beta \tan \gamma}
 \end{aligned}$$

7.4

$$\begin{aligned}
 \prod_p \left(1 - \frac{1}{p^2}\right) &= \prod_p \frac{1}{1 + \frac{1}{p^2} + \frac{1}{p^3} + \frac{1}{p^4} + \dots} \\
 &= \left(\prod_p \left(1 + \frac{1}{p^2} + \frac{1}{p^3} + \dots\right)\right)^{-1} \\
 &= \left(1 + \frac{1}{2^2} + \frac{1}{3^2} + \dots\right)^{-1} \\
 &= \frac{6}{\pi^2}
 \end{aligned}$$

