

ASSIGNMENT-CHAPTER 3

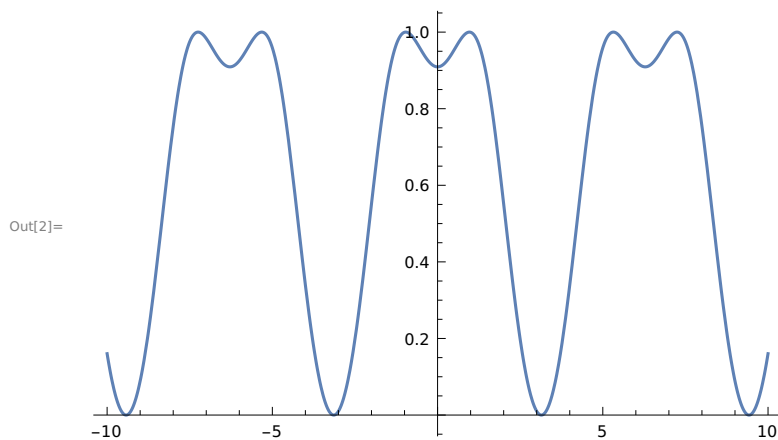
EXERCISES -3.2

1. Plot the following functions on the domain $-10 \leq x \leq 10$.

(a) $\sin(1+\cos(x))$

```
In[1]:= f[x_] := Sin[1 + Cos[x]]
```

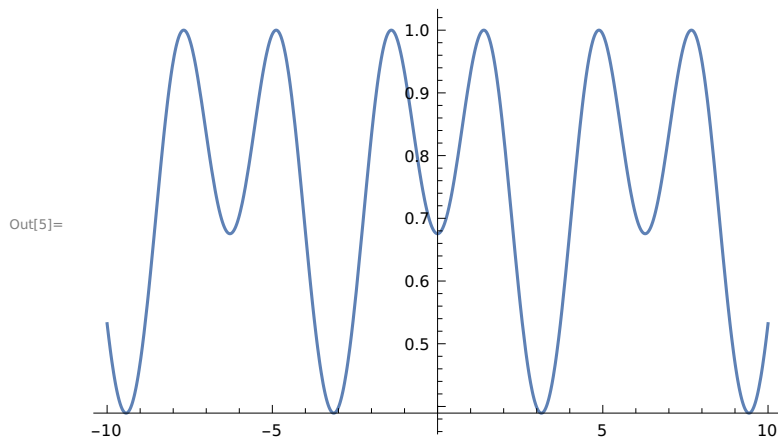
```
In[2]:= Plot[f[x], {x, -10, 10}]
```



(b) $\sin(1.4 + \cos(x))$

```
In[4]:= g[x_] := Sin[1.4 + Cos[x]]
```

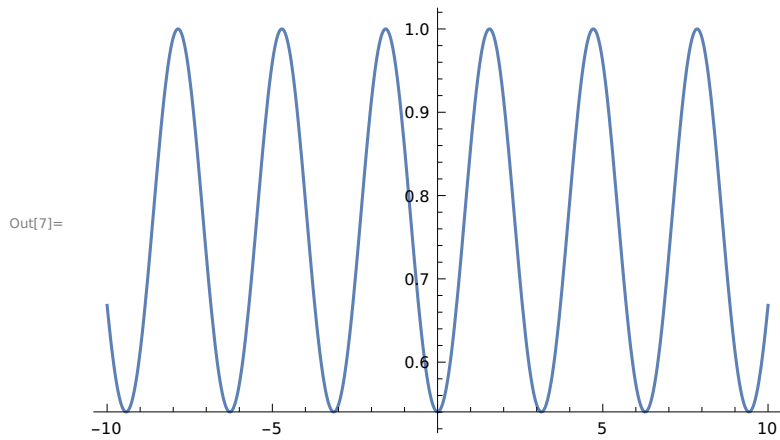
```
In[5]:= Plot[g[x], {x, -10, 10}]
```



(c) $\sin(\pi/2 + \cos(x))$

```
In[6]:= h[x_] := Sin[ $\pi/2 + \text{Cos}[x]$ ]
```

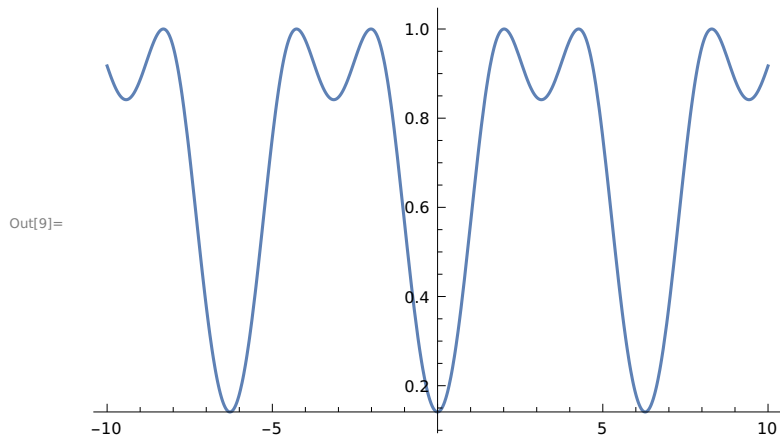
```
In[7]:= Plot[h[x], {x, -10, 10}]
```



(d) $\sin(2 + \cos(x))$

```
In[8]:= f[x_] := Sin[2 + Cos[x]]
```

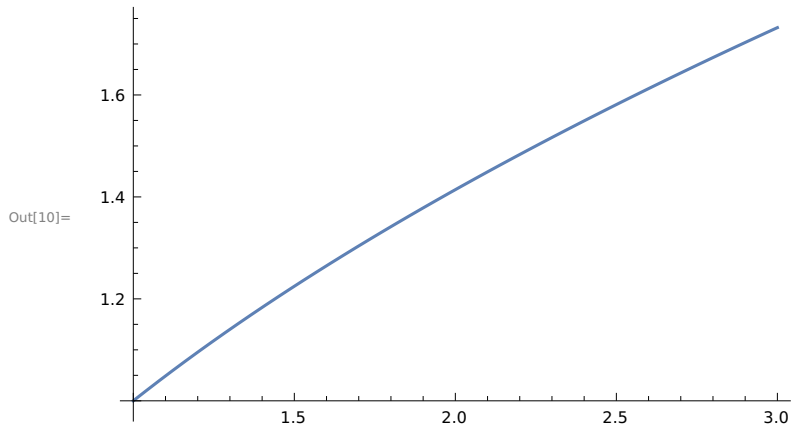
```
In[9]:= Plot[f[x], {x, -10, 10}]
```



2. Consider the square root function $f(x) = \sqrt{x}$ when x is near 2.

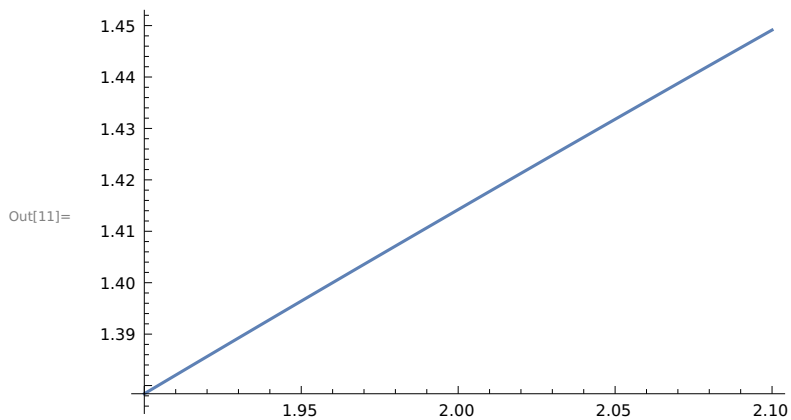
(a) Graph of f as x goes from 1 to 3.

In[10]:= `With[{ $\delta = 10^0$ }, Plot[\sqrt{x} , {x, 2 - δ , 2 + δ }]`

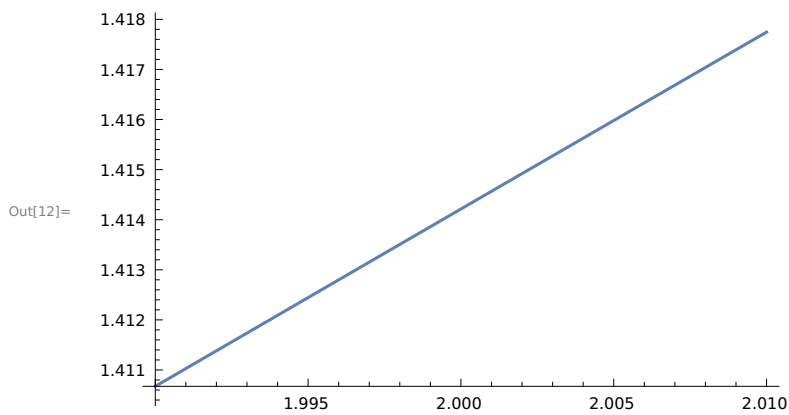


(b) Change the value of δ to be 10^{-1} , 10^{-2} , 10^{-3} and see the graph of f as x goes from 1.9 to 2.1

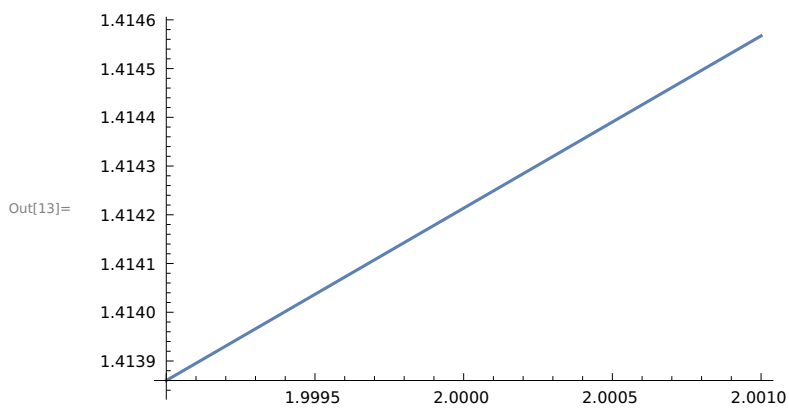
In[11]:= `With[{ $\delta = 10^{-1}$ }, Plot[\sqrt{x} , {x, 2 - δ , 2 + δ }]`



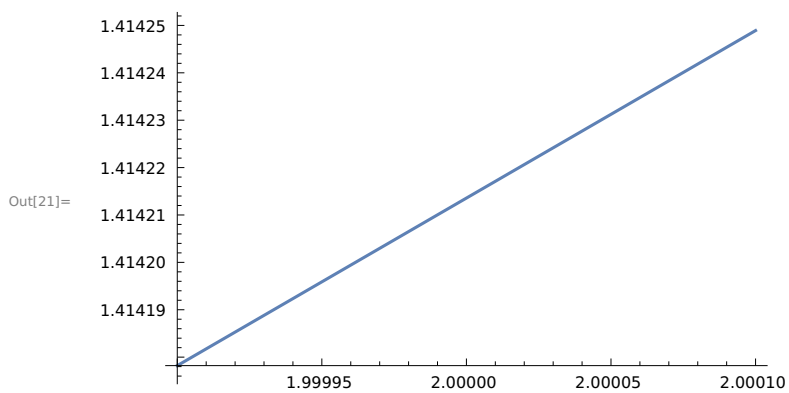
In[12]:= `With[{ $\delta = 10^{-2}$ }, Plot[\sqrt{x} , {x, 2 - δ , 2 + δ }]`



In[13]:= `With[{ $\delta = 10^{-3}$ }, Plot[\sqrt{x} , {x, 2 - δ , 2 + δ }]`



In[21]:= `With[{ $\delta = 10^{-4}$ }, Plot[\sqrt{x} , {x, 2 - δ , 2 + δ }]`



(c) Use the last plot to approximate $\sqrt{2}$ to six significant digits. Check your answer using `N`.

By the above plot we can approximate $\sqrt{2} = 1.41421$

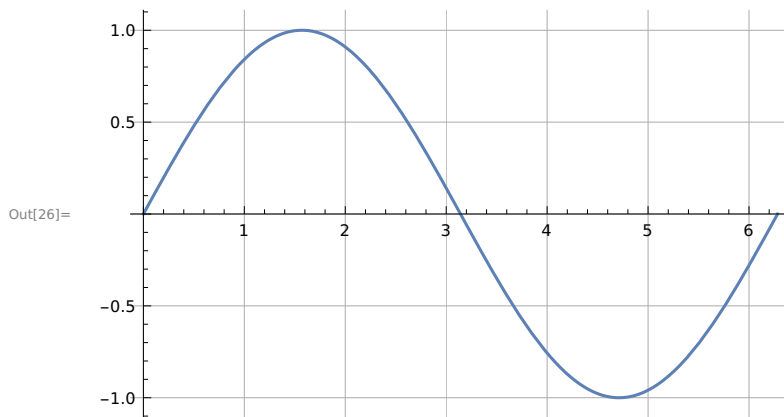
```
In[20]:= N[ $\sqrt{2}$ , 6]
```

```
Out[20]= 1.41421
```

EXERCISE -3.3

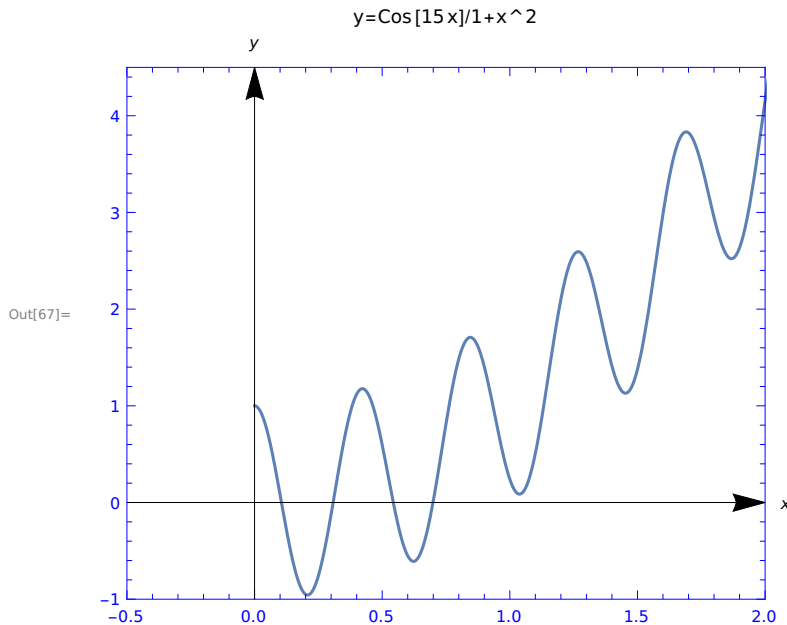
1. Use the `GridLines` and `Ticks` options, as well as the setting `GridLinesStyle`→`Lighter[Gray]` to plot the sine function.

```
In[26]:= Plot[Sin[x], {x, 0, 2  $\pi$ }, GridLines → Automatic,  
          Ticks → Automatic, GridLinesStyle → Lighter[Gray]]
```



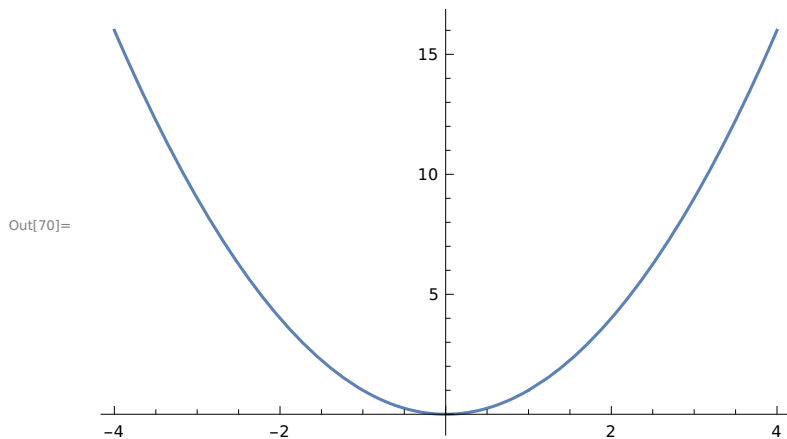
2. Use the Axes, Frame, Filling, FrameStyle, PlotRange and AspectRatio options to plot $y = \cos(15x)/1+x^2$

```
In[67]:= Plot[Cos[15 x]/1+x^2, {x, 0, π}, PlotRange → {{-0.5, 2}, {-1, 4.5}},
  Frame → True, AxesStyle → Arrowheads[00.05], AspectRatio → 5/6, Axes → True,
  AxesLabel → {x, y}, PlotLabel → "y=Cos[15x]/1+x^2", FrameStyle → Blue]
```



4. Plot the function $f(x) = x^2$ on the domain $-2 \leq x \leq 2$ and set Exclusions to $x=1$

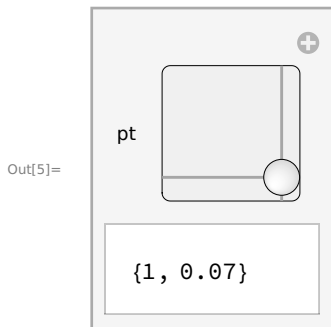
```
In[70]:= Plot[x^2, {x, -4, 4}, Exclusions → {x == 1}]
```



EXERCISES-3.4

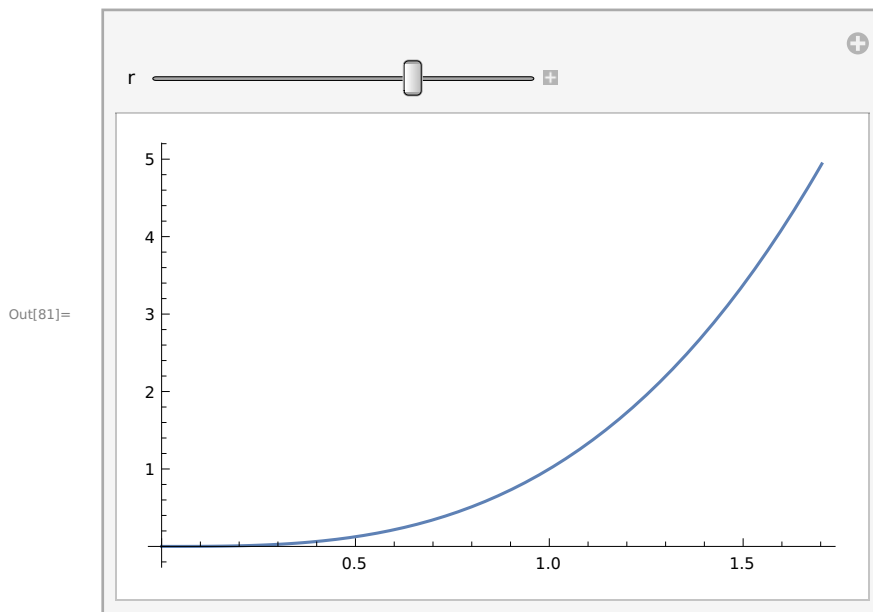
1. Make a Manipulate has output $\{x,y\}$, but has a single Slider2D controller.

In[5]:= `Manipulate[pt, {pt, {0, 0}, {1, 1}}`



2. Make a Manipulate of a Plot where the user can adjust the AspectRatio in real time from a starting value of $1/5$ to an ending value of 5. Set ImageSize to `{Automatic 128}` so the height remains constant as the slider is moved.

In[81]:= `Manipulate[Plot[x^3, {x, 0, r}], {r, 1, 2}, ImageSize -> {Automatic 128}, AspectRatio -> 5/6]`



EXERCISES -3.5

1. (a) Enter the followings inputs:

Range[100] and Partition[Range[100],10]

```
In[82]:= Range[100]
Out[82]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22,
  23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41,
  42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61,
  62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81,
  82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100}

In[83]:= Partition[Range[100], 10]
Out[83]= {{1, 2, 3, 4, 5, 6, 7, 8, 9, 10}, {11, 12, 13, 14, 15, 16, 17, 18, 19, 20},
  {21, 22, 23, 24, 25, 26, 27, 28, 29, 30}, {31, 32, 33, 34, 35, 36, 37, 38, 39, 40},
  {41, 42, 43, 44, 45, 46, 47, 48, 49, 50}, {51, 52, 53, 54, 55, 56, 57, 58, 59, 60},
  {61, 62, 63, 64, 65, 66, 67, 68, 69, 70}, {71, 72, 73, 74, 75, 76, 77, 78, 79, 80},
  {81, 82, 83, 84, 85, 86, 87, 88, 89, 90}, {91, 92, 93, 94, 95, 96, 97, 98, 99, 100}}
```

(b) Format a table for the first 100 integers, with twenty digits per row.

```
In[13]:= Partition[Range[100], 20]
Out[13]= {{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20},
  {21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40},
  {41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60},
  {61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80},
  {81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100}}
```

(c) Make a same table as above, but use only Table and Range commands.

```
In[25]:= Table[Range[20], 1]
  Table[Range[20, 40], 1]
Out[25]= {{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20}}
Out[26]= {{20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40}}
```

(d) Make a same table as above, but use only Table command (twice).

```
In[101]:= Table[x, {x, 1, 100}]
Out[101]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22,
  23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42,
  43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62,
  63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81,
  82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100}
```


4. (a) Use the Sum command to evaluate the following expression:

$$1^3+2^3+3^3+4^3+5^3+6^3+7^3+8^3+9^3+10^3+11^3+12^3+13^3+14^3+15^3+16^3+17^3+18^3+19^3+20^3$$

In[127]:= `f[x_] := x ^ 3`

In[128]:= `Sum[f[x], {x, 1, 20}]`

Out[128]= 44 100

(b) Make a Table of values for $x=1,2,\dots,10$ for the function

$f(x)$

$$=1^x+2^x+3^x+4^x+5^x+6^x+7^x+8^x+9^x+10^x+11^x+12^x+13^x+14^x+15^x+16^x+17^x+18^x+19^x+20^x$$

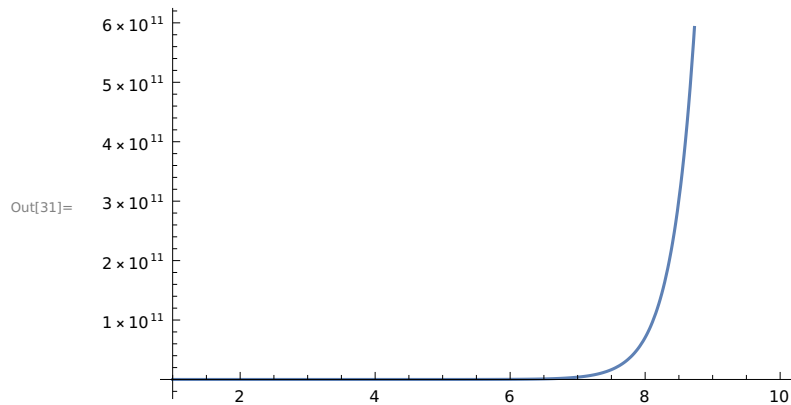
In[29]:= `f[x_] := 1 ^ x + 2 ^ x + 3 ^ x + 4 ^ x + 5 ^ x + 6 ^ x + 7 ^ x + 8 ^ x + 9 ^ x + 10 ^ x + 11 ^ x + 12 ^ x + 13 ^ x + 14 ^ x + 15 ^ x + 16 ^ x + 17 ^ x + 18 ^ x + 19 ^ x + 20 ^ x`

In[30]:= `Table[f[x], {x, 1, 10}]`

Out[30]= {210, 2870, 44 100, 722 666, 12 333 300, 216 455 810, 3 877 286 700, 70 540 730 666, 1 299 155 279 940, 24 163 571 680 850 }

(c) Plot $f(x)$ on the domain $1 \leq x \leq 10$.

In[31]:= `Plot[f[x], {x, 1, 10}]`

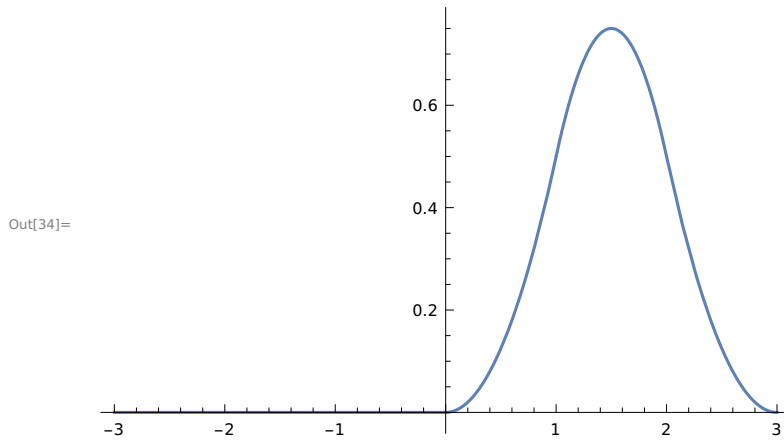


EXERCISES -3.6

2. Make a plot of a piecewise function.

```
In[33]:= f[x_] := Piecewise[{{0, x < 0}, {x^2/2, 0 ≤ x < 1},  
{-x^2 + 3x - 3/2, 1 ≤ x < 2}, {(1/2)(3 - x)^2, 2 ≤ x < 3}, {0, x ≤ 3}}]
```

```
In[34]:= Plot[f[x], {x, -3, 3}]
```



3. Make a plot of the step function.

```
In[23]:= f[x_] := Floor[x]
```

```
In[24]:= Plot[f[x], {x, 0, 20}]
```

