

# Chapter 3

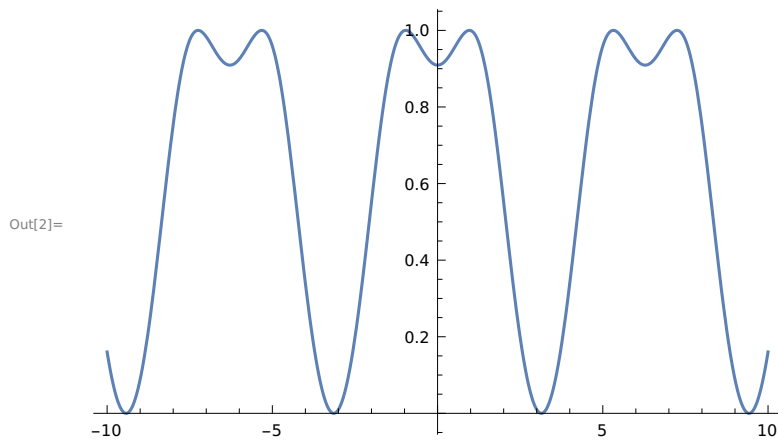
## Section 3.2

Question 1) Plot the following functions on the domain  $-10 \leq x \leq 10$ .

(a)  $f(x) = \text{Sin}[(1 + \text{Cos}[x])]$

```
In[1]:= f[x_] := Sin[(1 + Cos[x])]
```

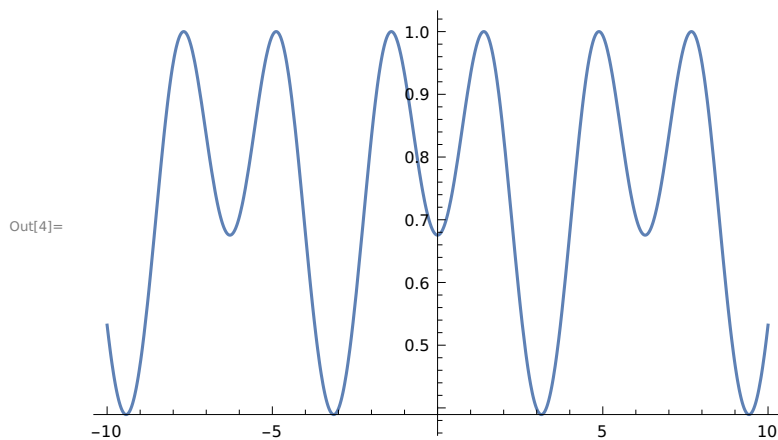
```
In[2]:= Plot[f[x], {x, -10, 10}]
```



(b)  $g(x) = \text{Sin}[(1.4 + \text{Cos}[x])]$

```
In[3]:= g[x_] := Sin[(1.4 + Cos[x])]
```

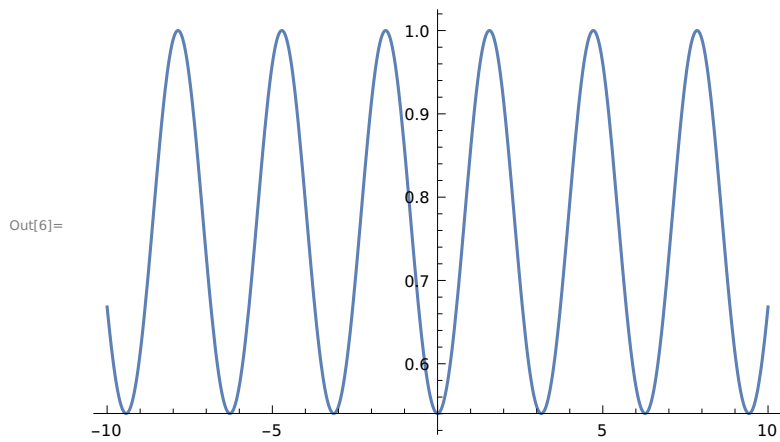
```
In[4]:= Plot[g[x], {x, -10, 10}]
```



(c)  $t(x) = \text{Sin}[(\text{Pi}/2 + \text{Cos}[x])]$

```
In[5]:= t[x_] := Sin[(Pi / 2 + Cos[x])]
```

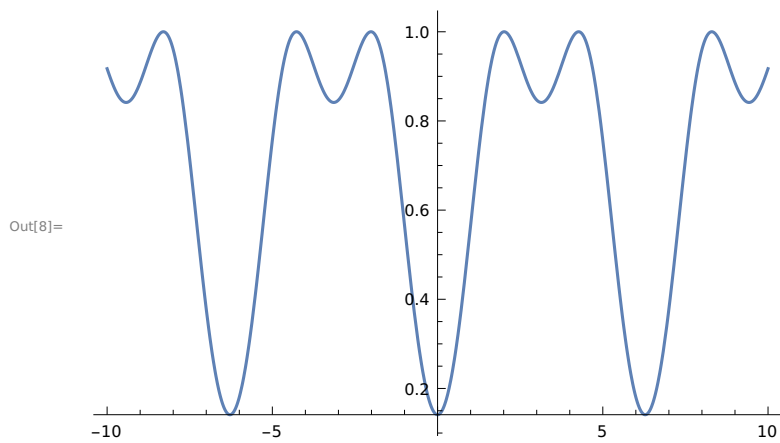
In[6]:= `Plot[t[x], {x, -10, 10}]`



(d)  $k(x) = \text{Sin}[(2 + \text{Cos}[x])]$

In[7]:= `k[x_] := Sin[(2 + Cos[x])]`

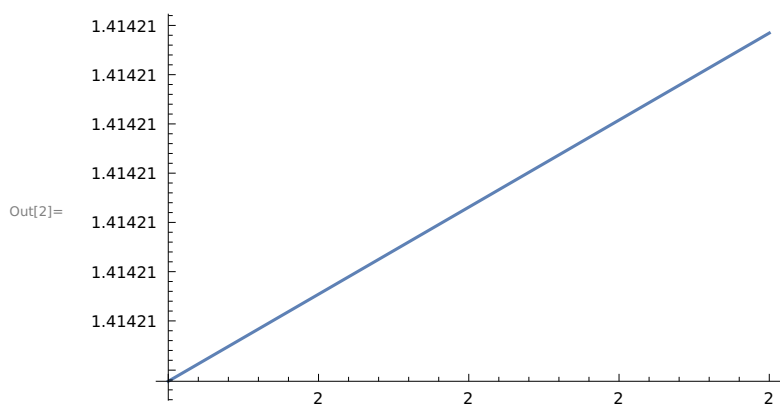
In[8]:= `Plot[k[x], {x, -10, 10}]`



Question 2) Consider function  $f(x) = (x)^{1/2}$  when  $x$  is near 2

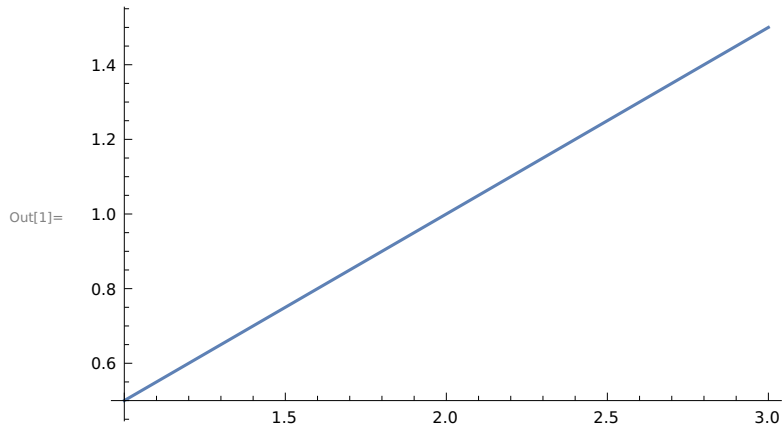
In[1]:= `f[x_] := x^(1/2)`

In[2]:= `With[{δ = 10^(-10)}, Plot[f[x], {x, 2 - δ, 2 + δ}]]`



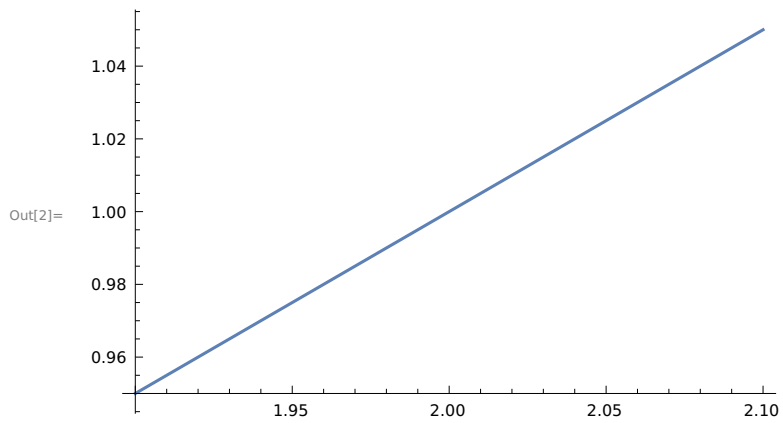
(a) Enter the input to see the graph of  $f$  as  $x$  goes from 1 to 3

```
In[1]:= With[{ $\delta = 10^0$ }, Plot[x1/2, {x, 2 -  $\delta$ , 2 +  $\delta$ }]
```

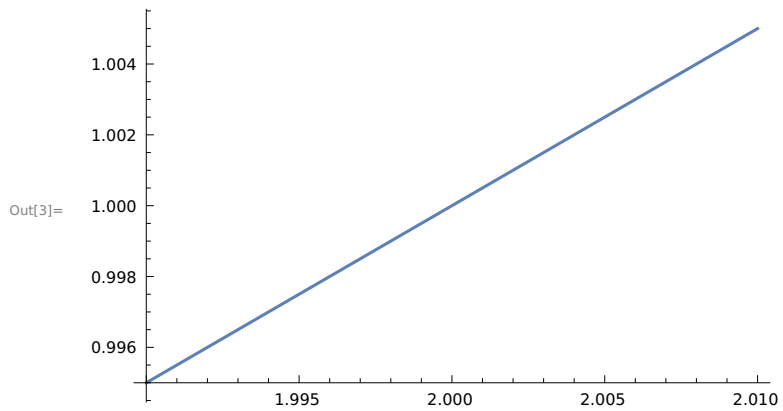


(b)

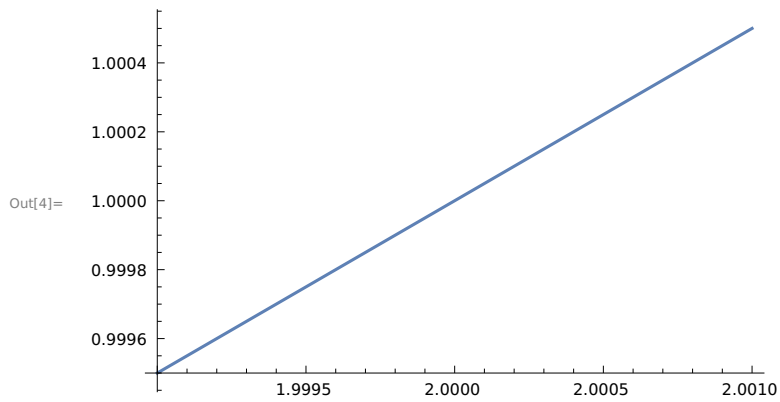
```
In[2]:= With[{ $\delta = 10^{-1}$ }, Plot[x1/2, {x, 2 -  $\delta$ , 2 +  $\delta$ }]
```



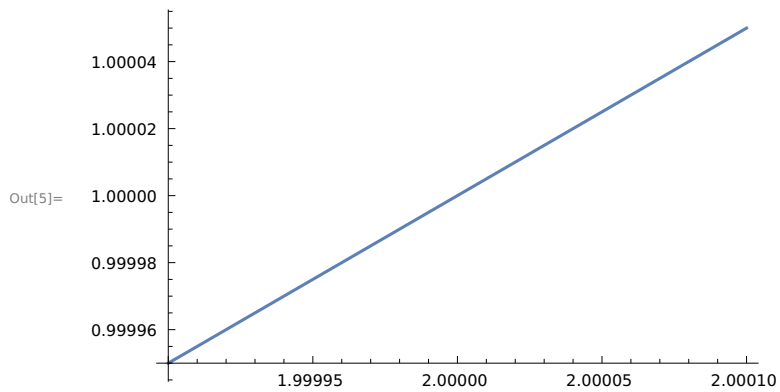
```
In[3]:= With[{ $\delta = 10^{-2}$ }, Plot[x1/2, {x, 2 -  $\delta$ , 2 +  $\delta$ }]
```



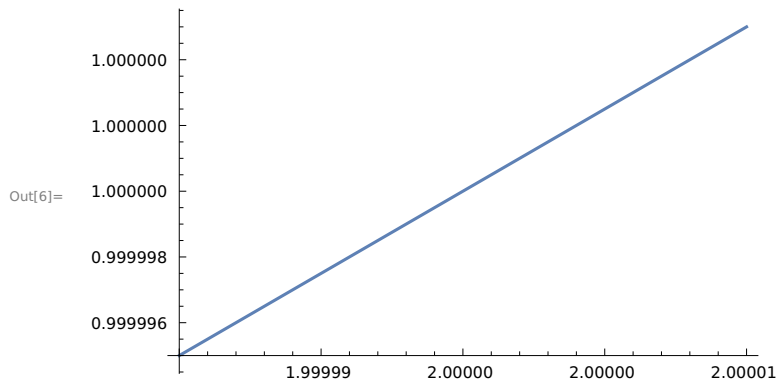
In[4]:= `With[{ $\delta = 10^{-3}$ }, Plot[x1/2, {x, 2 -  $\delta$ , 2 +  $\delta$ }]`



In[5]:= `With[{ $\delta = 10^{-4}$ }, Plot[x1/2, {x, 2 -  $\delta$ , 2 +  $\delta$ }]`



In[6]:= `With[{ $\delta = 10^{-5}$ }, Plot[x1/2, {x, 2 -  $\delta$ , 2 +  $\delta$ }]`

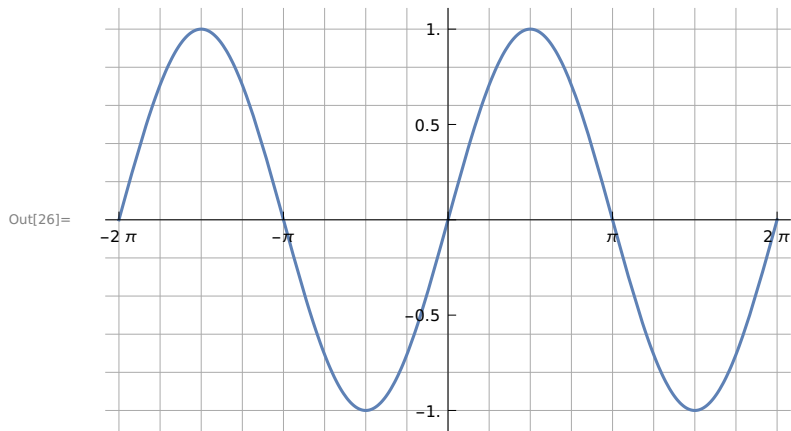


## Section 3.3

Question 1) Plot the Sin function using the Gridlines and Ticks option

In[25]:= `f[x_] := Sin[x]`

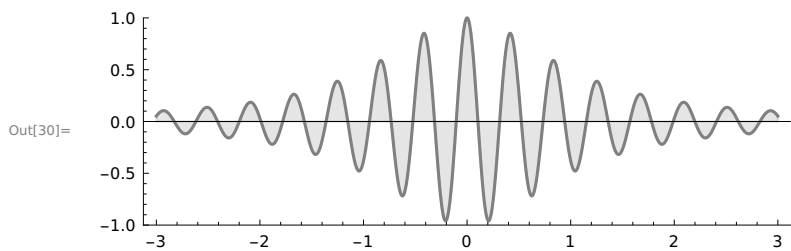
```
In[26]:= Plot[f[x], {x, -2 Pi, 2 Pi}, GridLines -> {Range[-2 Pi, 2 Pi, Pi/4], Range[-1, 1, 0.2]},
  Ticks -> {Range[-2 Pi, 2 Pi, Pi], Range[-1, 1, 0.5]}, GridLinesStyle -> Lighter[Gray]]
```



Question 2) Plot the function  $\text{Cos}[15 x]/(1+x^2)$  using Axes,Frame,Filling, Plot Range and Aspect Ratio.

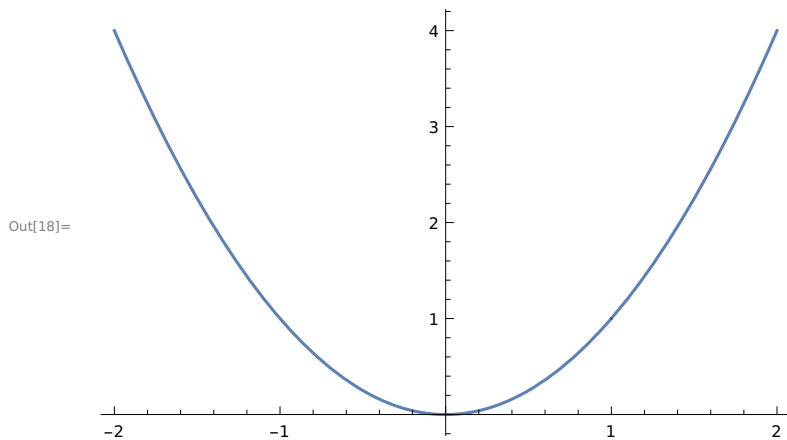
```
In[28]:= f[x_] := Cos[15 x] / (1 + x ^ 2)
```

```
In[30]:= Plot[f[x], {x, -3, 3}, Axes -> {True, False}, AspectRatio -> Automatic ,
  Filling -> Axis, Frame -> {{True, False}, {True, False}},
  FrameStyle -> {Gray}, PlotStyle -> {Gray}, PlotRange -> {-1, 1}]
```



Question 4) Plot the function  $x^2$  on the domain  $-2 \leq x \leq 2$  and set Exclusions to  $\{x == 1\}$ . Note that  $f$  has no vertical asymptote at  $x = 1$ .

In[18]:= `Plot[x^2, {x, -2, 2}, Exclusions -> {x == 1}, ExclusionsStyle -> Dashed]`

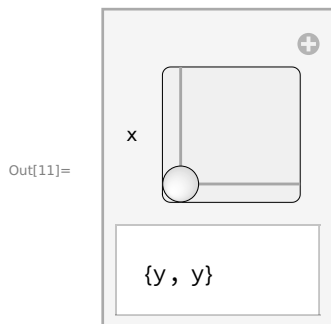


This function has no asymptote at  $x = 1$ .

## Section 3.4

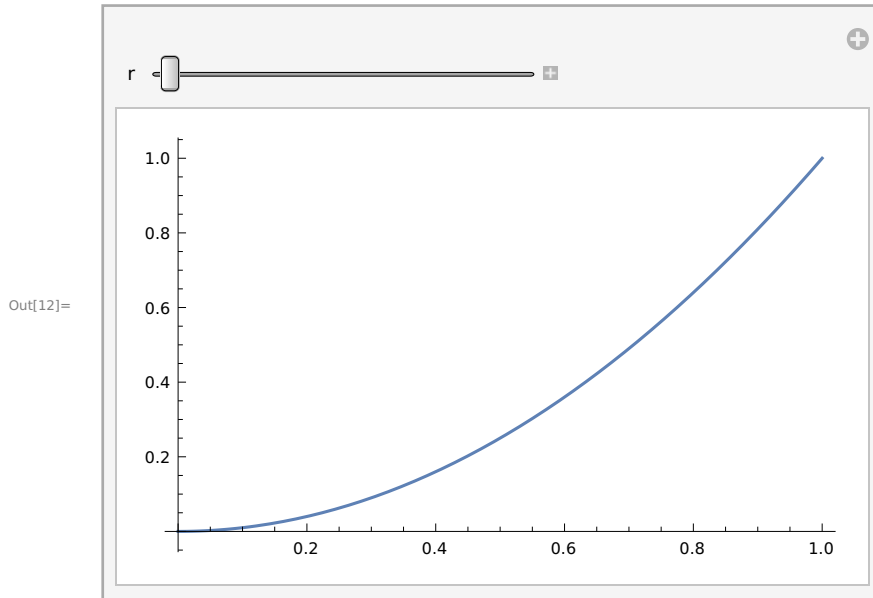
Question 1) Make a manipulate that also has output  $\{x,y\}$  but that has a single Slider 2D Controller.

In[11]:= `Manipulate[{x, y}, {x, y, {0, 1}}`



Question 2) Make a Manipulate of a Plot where the user can adjust the Aspect Ratio in real time, from a starting value of  $1/5$  (five times as wide as it is tall) to an ending value of  $5$ . Set ImageSize to `{Automatic, 128}` so the height remains constant as the slider is moved.

In[12]:= `Manipulate[Plot[x^2, {x, 0, r}], {r, 1, 3}, ImageSize -> {Automatic, 128}, AspectRatio -> 5 / 6]`



## Section 3.5

### Question 1)

(a) Enter the following inputs and discuss the outputs

In[8]:= `Range[100]`

Out[8]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100}

In[4]:= `Partition[Range[100], 10]`

Out[4]= {{1, 2, 3, 4, 5, 6, 7, 8, 9, 10}, {11, 12, 13, 14, 15, 16, 17, 18, 19, 20}, {21, 22, 23, 24, 25, 26, 27, 28, 29, 30}, {31, 32, 33, 34, 35, 36, 37, 38, 39, 40}, {41, 42, 43, 44, 45, 46, 47, 48, 49, 50}, {51, 52, 53, 54, 55, 56, 57, 58, 59, 60}, {61, 62, 63, 64, 65, 66, 67, 68, 69, 70}, {71, 72, 73, 74, 75, 76, 77, 78, 79, 80}, {81, 82, 83, 84, 85, 86, 87, 88, 89, 90}, {91, 92, 93, 94, 95, 96, 97, 98, 99, 100}}

(b) Format a table of 100 integers, with 20 digits per row.

```
In[13]:= Grid[Partition[Range[100], 20]]
      1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20
      21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40
Out[13]:= 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60
      61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80
      81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100
```

(c) Make the same table as above , but use only the table and range commands. Do not use Partition.

```
In[14]:= Grid[Table[Range[x, x + 19], {x, {1, 21, 41, 61, 81}}]]
      1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20
      21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40
Out[14]:= 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60
      61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80
      81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100
```

(d) Make the same table as above but use only Table command (twice) .

```
In[31]:= f[x_] := x
In[33]:= Grid[Table[Table[f[x], {x, x, x + 19}], {x, {1, 21, 41, 61, 81}}]]
      1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20
      21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40
Out[33]:= 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60
      61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80
      81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100
```

#### Question 4)

(a) Use the Sum command to evaluate the following expression

```
In[10]:= f[x_] := x ^ 3
In[11]:= Sum[f[x], {x, 1, 20}]
Out[11]= 44 100
```

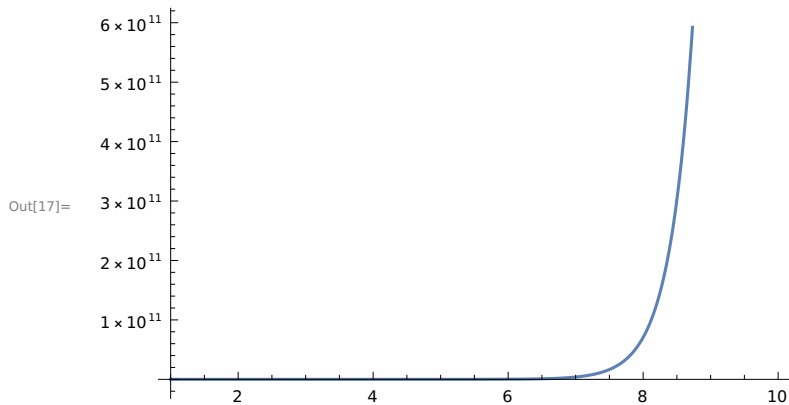
(b) Make the table of values for  $x = 1, 2, \dots, 10$  for the function  $f(x) = 1+2^x+3^x+4^x+5^x+6^x+7^x+8^x+9^x+10^x+11^x+12^x+13^x+14^x+15^x+16^x+17^x+18^x+19^x+20^x$

```
In[15]:= g[x_] := 1 + 2 ^ x + 3 ^ x + 4 ^ x + 5 ^ x + 6 ^ x + 7 ^ x + 8 ^ x + 9 ^ x + 10 ^ x +
      11 ^ x + 12 ^ x + 13 ^ x + 14 ^ x + 15 ^ x + 16 ^ x + 17 ^ x + 18 ^ x + 19 ^ x + 20 ^ x
In[16]:= Table[g[x], {x, 1, 10}]
Out[16]= {210, 2870, 44 100, 722 666, 12 333 300, 216 455 810,
      3 877 286 700, 70 540 730 666, 1 299 155 279 940, 24 163 571 680 850 }
```



(c) Plot this function on the domain  $1 \leq x \leq 10$

In[17]:= `Plot[g[x], {x, 1, 10}]`



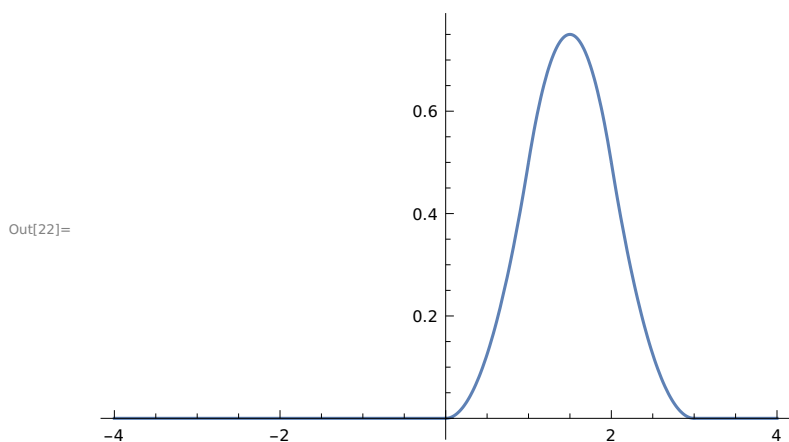
## Section 3.6

Question 2 ) Make a Plot of the Piecewise function

$$f(x) = \begin{cases} 0 & x < 0; \\ x^2 / 2 & 0 \leq x < 1; \\ -x^2 + 3x - 3/2 & 1 \leq x < 2; \\ 1/2 (3-x)^2 & 2 \leq x < 3; \\ 0 & 3 \leq x; \end{cases}$$

In[17]:= `f[x_] := Piecewise[{{0, (x < 0) || (3 ≤ x)}, {(x^2)/2, 0 ≤ x < 1},  
{{-(x^2) + 3 x - 3/2}, 1 ≤ x < 2}, {(1/2) * (3 - x)^2, 2 ≤ x < 3}}]`

In[22]:= `Plot[f[x], {x, -4, 4}]`



Question 3) A Step Function assumes a constant value between consecutive integers  $n$  and  $n+1$ . Make a plot of the step function  $f(x)$  whose value is  $n^2$  when  $n \leq x < n+1$ . Use the domain  $0 \leq x < 20$ .

```
In[22]:= f[x_] := Piecewise[{{n^2, n ≤ x < n+1}, {1, n ≤ x ≤ n+1}}
```

```
In[23]:= Plot[f[x], {x, 0, 20}]
```

Out[23]=

