

# CHAPTER 3- TORRENCE

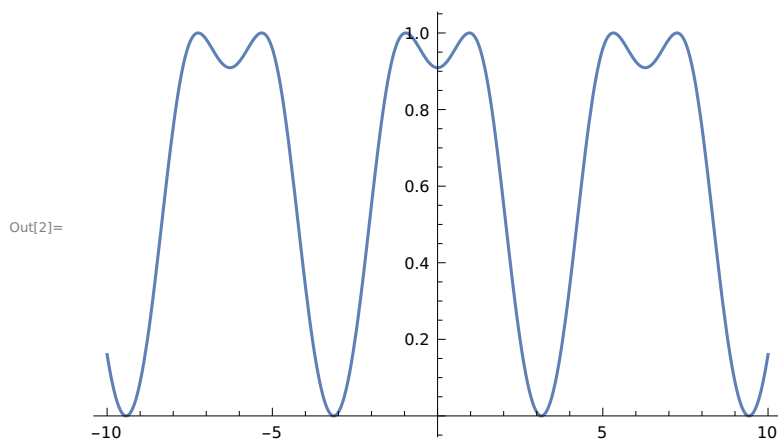
## ■ SECTION 3.2

QUES.1 Plot the following functions on the domain  $-10 \leq x \leq 10$ .

a.  $\sin(1+\cos(x))$

```
In[1]:= f[x_] := Sin[1 + Cos[x]]
```

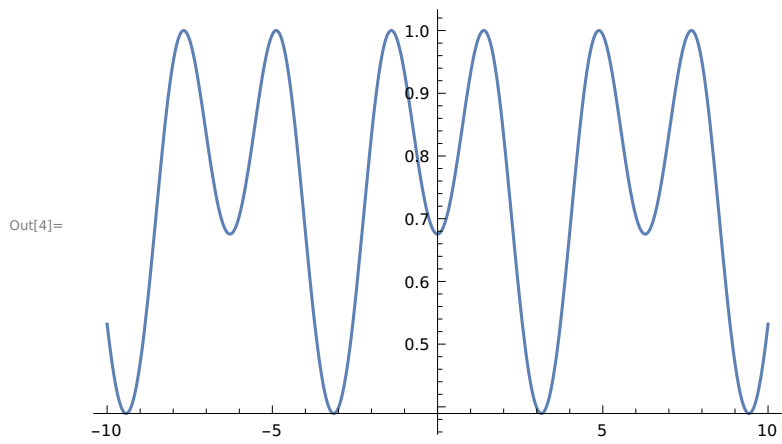
```
In[2]:= Plot[f[x], {x, -10, 10}]
```



b.  $\sin(1.4+\cos(x))$

```
In[3]:= f[x_] := Sin[1.4 + Cos[x]]
```

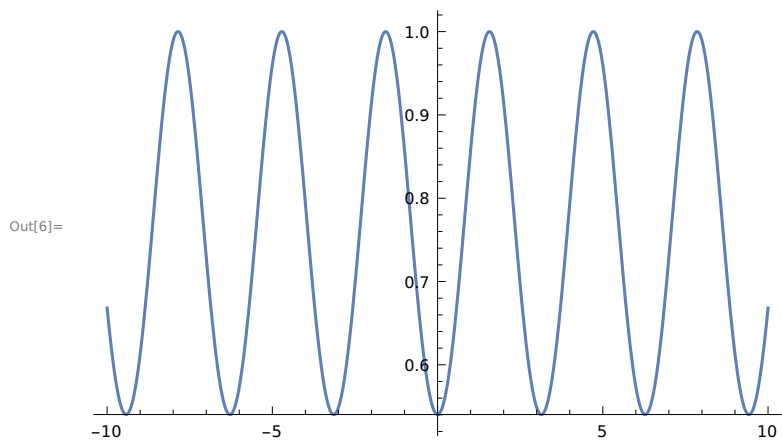
In[4]:= `Plot[f[x], {x, -10, 10}]`



c.  $\sin(\pi/2 + \cos(x))$

In[5]:= `f[x_] := Sin[pi/2 + Cos[x]]`

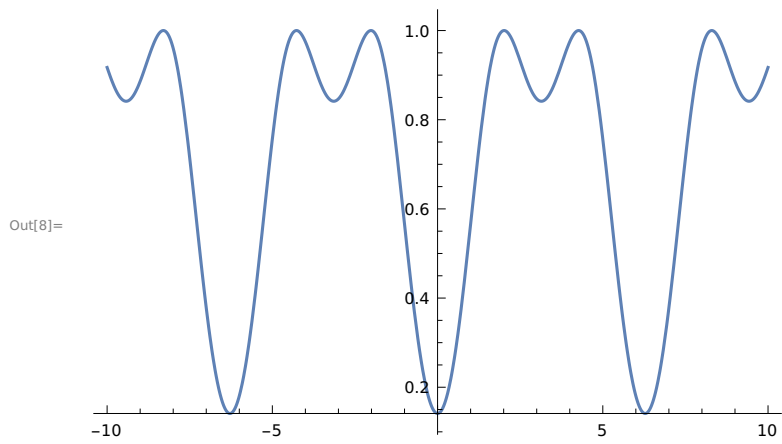
In[6]:= `Plot[f[x], {x, -10, 10}]`



d.  $\sin(2 + \cos(x))$

In[7]:= `f[x_] := Sin[2 + Cos[x]]`

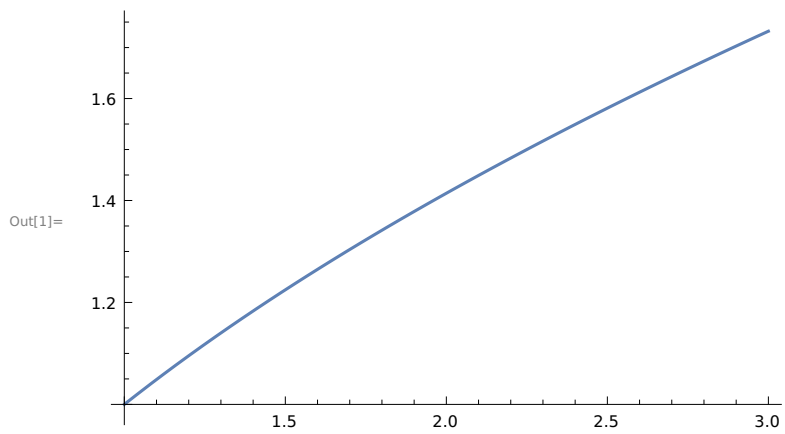
In[8]:= `Plot[f[x], {x, -10, 10}]`



## Ques. 2

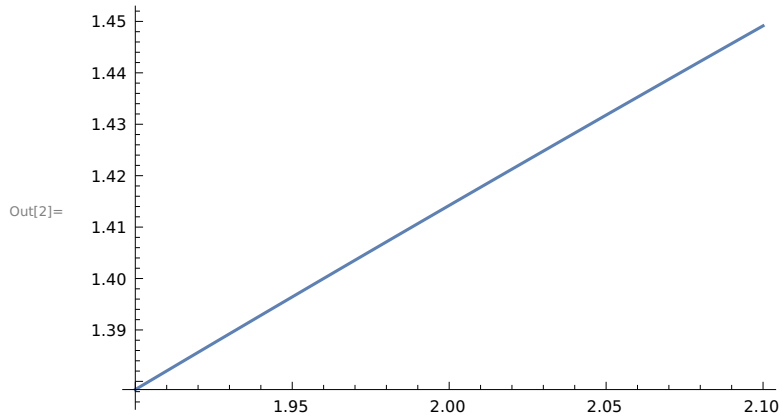
a.

In[1]:= `With[{ $\delta = 10^{-6}$ }, Plot[ $\sqrt{x}$ , {x, 2 -  $\delta$ , 2 +  $\delta$ }]`



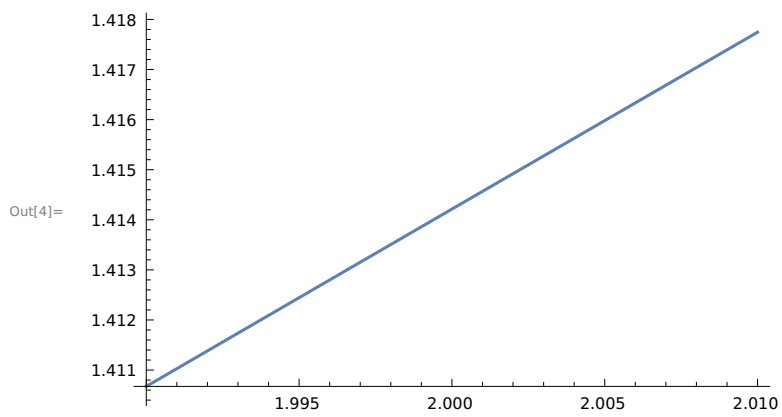
b.  $\delta=10^{-1}$

```
In[2]:= With[{ $\delta = 10^{-1}$ }, Plot[ $\sqrt{x}$ , {x, 2 -  $\delta$ , 2 +  $\delta$ }]]
```



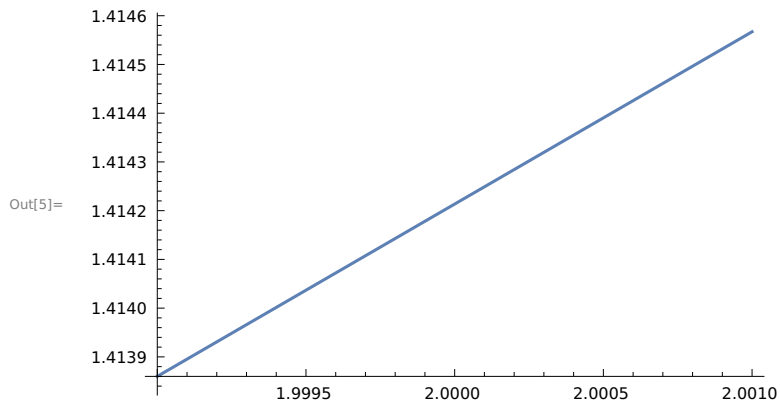
$\delta=10^{-2}$

```
In[4]:= With[{ $\delta = 10^{-2}$ }, Plot[ $\sqrt{x}$ , {x, 2 -  $\delta$ , 2 +  $\delta$ }]]
```



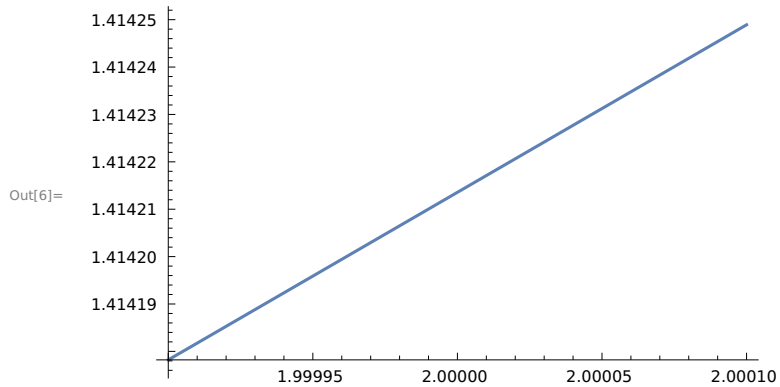
$$\delta = 10^{-3}$$

In[5]:= `With[{ $\delta = 10^{-3}$ }, Plot[ $\sqrt{x}$ , {x, 2 -  $\delta$ , 2 +  $\delta$ }]`



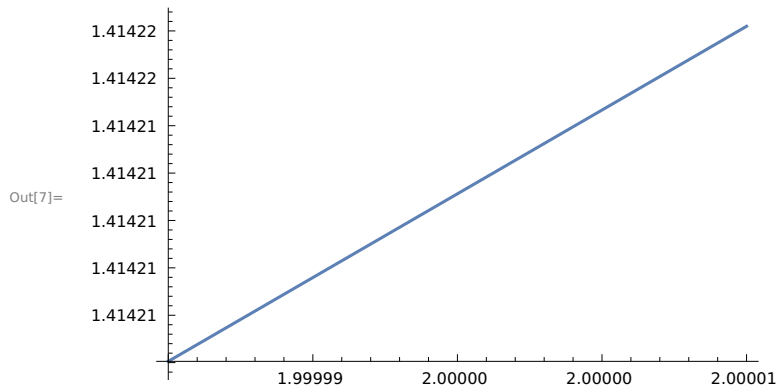
$$\delta = 10^{-4}$$

In[6]:= `With[{ $\delta = 10^{-4}$ }, Plot[ $\sqrt{x}$ , {x, 2 -  $\delta$ , 2 +  $\delta$ }]`



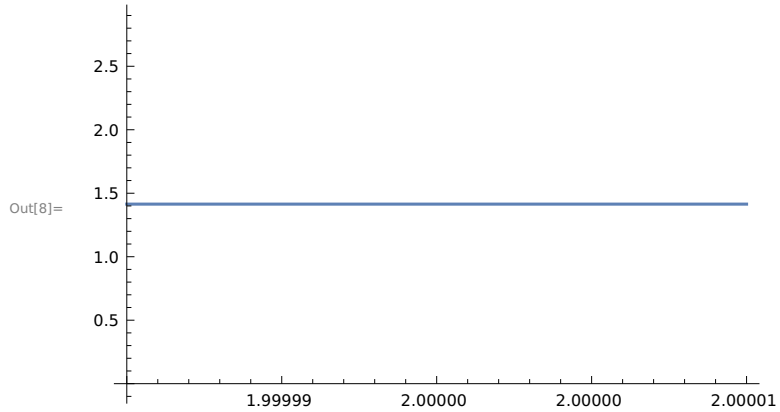
$$\delta = 10^{-5}$$

In[7]:= `With[{ $\delta = 10^{-5}$ }, Plot[ $\sqrt{x}$ , {x, 2 -  $\delta$ , 2 +  $\delta$ }]`



c.  $\sqrt{2}$ 

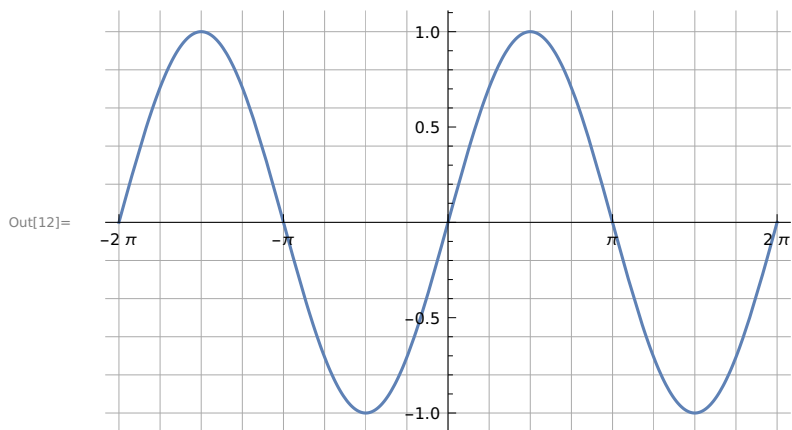
```
In[8]:= With[{ $\delta = 10^{-5}$ }, Plot[ $\sqrt{2}$ , {x, 2 -  $\delta$ , 2 +  $\delta$ }]]
```



## SECTION 3.3

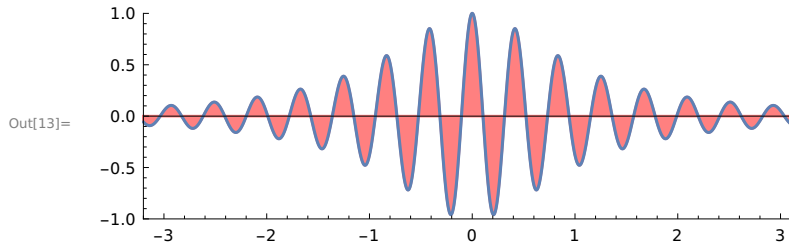
Ques 1.

```
In[12]:= Plot[Sin[x], {x, -2 Pi, 2 Pi}, GridLinesStyle -> Lighter[Gray],
  GridLines -> {Range[-2 Pi, 2 Pi, Pi / 4], Range[-1, 1, 0.2]},
  Ticks -> {Range[-2 Pi, 2 Pi, Pi], Automatic}]
```



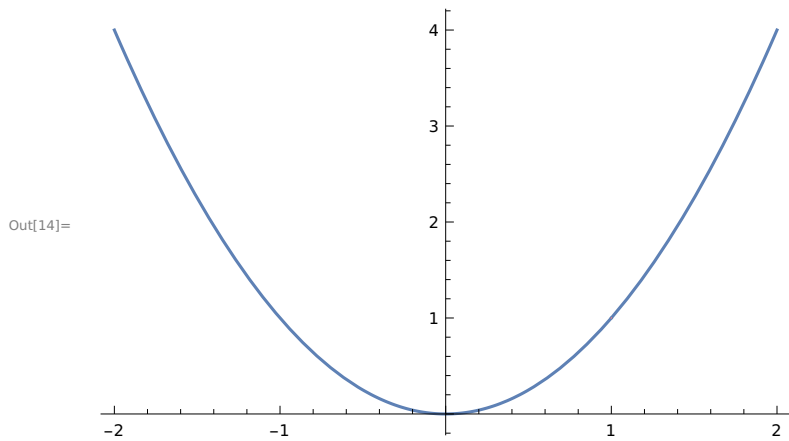
## Ques. 2

```
In[13]:= Plot[(Cos[15 x])/(1 + x^2), {x, -3.2, 3.2}, AspectRatio -> Automatic ,
  AxesOrigin -> {-3, 0}, Frame -> {{True, False}, {True, False}}, Axes -> {x, y},
  PlotRange -> {{-3.2, 3.1}, {-1, 1}}, Filling -> Axis, FillingStyle -> Pink]
```



## Ques. 4

```
In[14]:= Plot[x^2, {x, -2, 2}, Exclusions -> {x == 1}, ExclusionsStyle -> Directive[Pink, Dashed]]
```

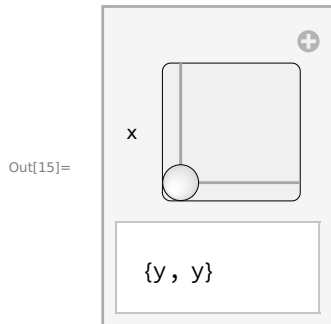


There is no vertical asymptote, this shows that the graph is continuous.

## SECTION 3.4

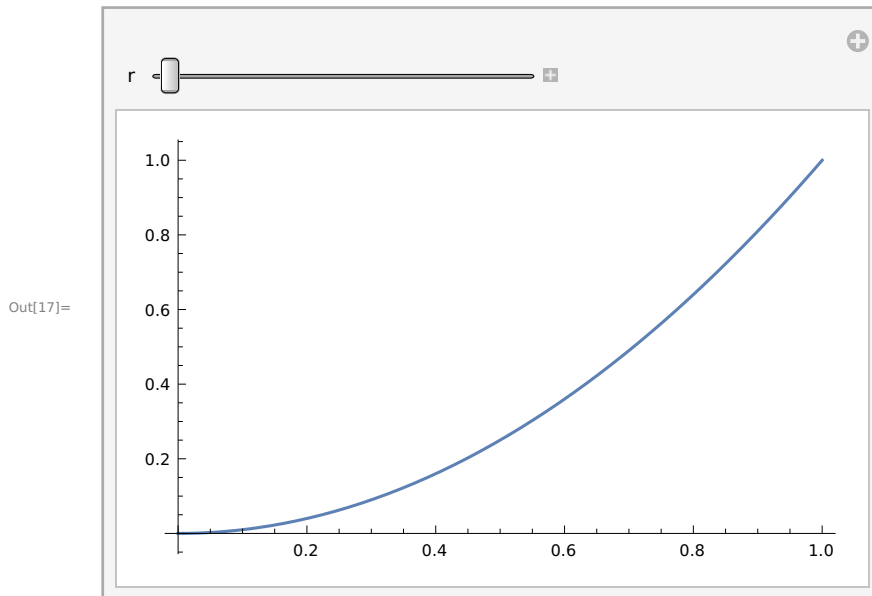
### Ques. 1

```
In[15]:= Manipulate[{x, y}, {x, y, {0, 1}}
```



### Ques. 2

```
In[17]:= Manipulate[Plot[x^2, {x, 0, r}], {r, 1, 3},  
ImageSize -> {Automatic, 128}, AspectRatio -> 5/6]
```



## SECTION 3.5

### Ques.1

a.



In[18]:= **Range[100]**

Out[18]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22,  
23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41,  
42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61,  
62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81,  
82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100}

In[19]:= **Partition[Range[100], 10]**

Out[19]= {{1, 2, 3, 4, 5, 6, 7, 8, 9, 10}, {11, 12, 13, 14, 15, 16, 17, 18, 19, 20},  
{21, 22, 23, 24, 25, 26, 27, 28, 29, 30}, {31, 32, 33, 34, 35, 36, 37, 38, 39, 40},  
{41, 42, 43, 44, 45, 46, 47, 48, 49, 50}, {51, 52, 53, 54, 55, 56, 57, 58, 59, 60},  
{61, 62, 63, 64, 65, 66, 67, 68, 69, 70}, {71, 72, 73, 74, 75, 76, 77, 78, 79, 80},  
{81, 82, 83, 84, 85, 86, 87, 88, 89, 90}, {91, 92, 93, 94, 95, 96, 97, 98, 99, 100}}

The `Range[100]` command displays numbers from 1 to 100 where as the command `Partition[Range[100],10]` displays the numbers from 1 to 100 while simultaneously segregating them in a list 8 of 10 numbers

b.

In[20]:= **Grid[Partition[Range[100], 20]]**

Out[20]= 

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100

c.

In[21]:= **Grid[Table[Range[x, x + 19], {x, {1, 21, 41, 61, 81}}]]**

Out[21]= 

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100

d.

In[4]:= **f[x\_] := x**In[5]:= **Grid[Table[Table[f[x], {x, x, x + 19}], {x, {1, 21, 41, 61, 81}}]**

```

      1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16 17 18 19 20
      21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40
Out[5]= 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60
      61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80
      81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100

```

Ques. 4

a.

In[6]:= **f[x\_] := x ^ 3**In[7]:= **Sum[f[x], {x, 1, 20}]**

Out[7]= 44 100

b.

```

In[8]:= f[x_] := 1 + 2 ^ x + 3 ^ x + 4 ^ x + 5 ^ x + 6 ^ x + 7 ^ x + 8 ^ x + 9 ^ x + 10 ^ x +  

11 ^ x + 12 ^ x + 13 ^ x + 14 ^ x + 15 ^ x + 16 ^ x + 17 ^ x + 18 ^ x + 19 ^ x + 20 ^ x

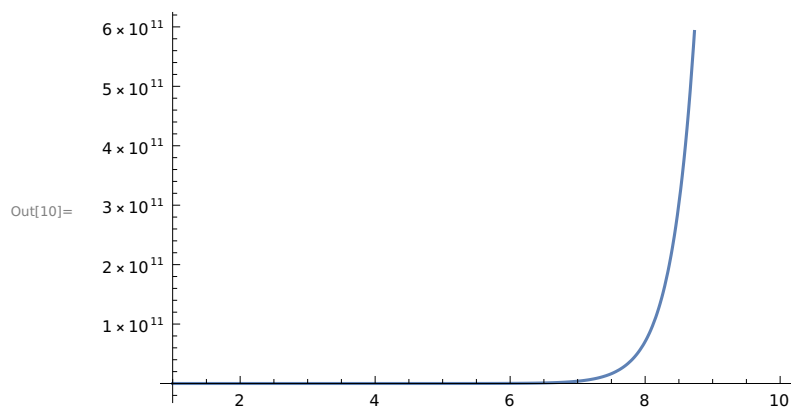
```

In[9]:= **Table[f[x], {x, 1, 10}]**

```

Out[9]= {210, 2870, 44 100, 722 666, 12 333 300, 216 455 810,
3 877 286 700, 70 540 730 666, 1 299 155 279 940, 24 163 571 680 850 }

```

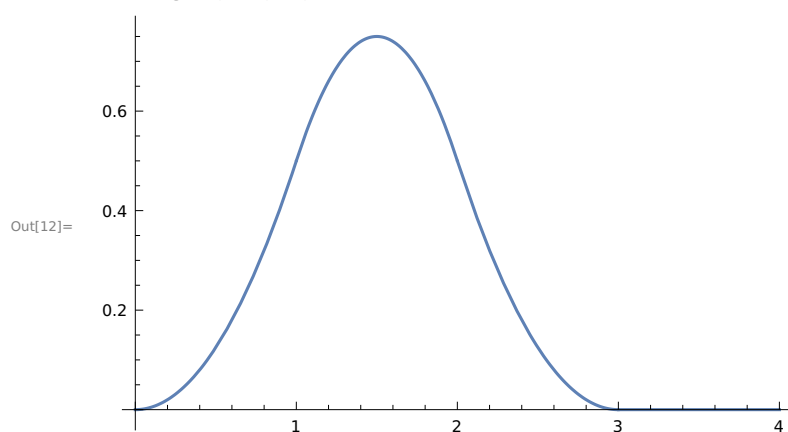
In[10]:= **Plot[f[x], {x, 1, 10}]**

## SECTION 3.6

### Ques.2

```
In[11]:= g[x_] := Piecewise[{{0, x < 0}, {(x^2)/2, 0 ≤ x ≤ 1},
    {-x^2 + 3x - 3/2, 1 ≤ x < 2}, {1/2(3-x)^2, 2 ≤ x < 3}, {0, 3 ≤ x}}]
```

```
In[12]:= Plot[g[x], {x, 0, 4}]
```



### Ques. 3

```
In[15]:= f[x_, n_] := Piecewise[{{n^2, n ≤ x ≤ n + 1}}]
```

```
In[16]:= Plot[f[x, n], {x, 0, 20}]
```

