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1 \documentclass[10pt]{beamer} Add comment
2 \usepackage[utf8]{inputenc}
3
4
5 \title{Assignment 2}
6 \author{Shruti Kaushik\\ 20044563021\\
    MAT/20/85}
7 \institute{\Large Mata Sundri College For
    Women\\
    University of Delhi}
8 \date{}
9 \usetheme{Copenhagen}
10
11
12 \begin{document}
13 \begin{frame}
14 \begin{minipage}{0.13\textwidth}
15 \includegraphics[width=2cm,height=2cm]{MSC
    W logo.png}
16 \end{minipage}\hfill
17 \begin{minipage}{0.13\textwidth}
18 \includegraphics[width=2.5cm,height=2cm]{8
    0759944.jpg}
19 \end{minipage}
20 \maketitle
21 \end{frame}
22 \setbeamertemplate{background}{\includegra
    phics[width=\paperwidth,height=\paperheigh
    t]{background 2.jpg}}
23 \begin{frame}{Example}
24 \begin{block}
25
26
27 Let  $\mathbf{x}=(x_1, \dots, x_n)$ 
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28      where the  $x_i$ s are non negative real
29      numbers.
30      Set
31       $M_r(\mathbf{x}) = \left( \frac{x_1^r + x_2^r + \dots + x_n^r}{n} \right)^{1/r}$ , \\
32      ;  $r \in \mathbf{R} \setminus \{0\}$ , \\
33      and
34       $M_0(\mathbf{x}) = (x_1 x_2 \dots x_n)^{1/n}$ .
35      We call  $M_r(\mathbf{x})$  the
36      power mean of
37       $\mathbf{x}$ . \\
38  \begin{frame}
39  \begin{block}
40
41      Define
42       $V_n =$ 
43      
$$\begin{array}{cccccc}
44          1 & 1 & 1 & \dots & 1 & \\
45          x_1 & x_2 & x_3 & \dots & x_n & \\
46          x_1^2 & x_2^2 & x_3^2 & \dots & x_n^2 & \\
47          \vdots & \vdots & \vdots & \ddots & \vdots & \\
48          x_1^{n-1} & x_2^{n-1} & x_3^{n-1} & \dots & x_n^{n-1} & \\
49      \end{array}$$

50      We call  $V_n$  the Vandermonde
51      matrix of order  $n$ . \\
52      Claim:  $\det V_n = \prod_{1 \leq i < j \leq n} (x_j - x_i)$ 
53  \end{block}
54  \begin{frame}{Question 4.}
55  
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55 -> \begin{block}
56
57     \item $$3^3 + 4^3 + 5^3=6^3$$
58 \end{block}
59 -> \begin{block}
60
61     \item $$\sqrt{100} = 10$$
62 \end{block}
63 -> \begin{block}
64
65     \item $$(a+b)^3=a^3+3a^2b+3ab^2+b^3$$
66 \end{block}
67 -> \begin{block}
68
69     \item $\sum_{k=1}^n k=\frac{n(n+1)}{2}$
70 \end{block}
71 -> \begin{block}
72
73     \item $\frac{\pi}{4}=\frac{1}{1}-\frac{1}{3}+\frac{1}{5}-\frac{1}{7}+\frac{1}{9}-\frac{1}{11}+\dots$]
74 \end{block}
75 \end{frame}
76 -> \begin{frame}{Remaining Parts of Question 4}
77 -> \begin{block}
78
79     \item $cos\theta=sin(90^\circ-\theta)$
80 \end{block}
81 -> \begin{block}
82
83     \item $e^{i\theta} = cos\theta + isin\theta$
84 \end{block}
85 -> \begin{block}
86
87     \item $\lim_{\theta\rightarrow 0}\frac{s\theta}{\theta}=1.$
88 \end{block}
89 -> \begin{block}
90
91     \item $\lim_{x\rightarrow\infty}\frac{\pi(x)}{x/\log x}=1$
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92 \end{block}
93 \begin{block}
94
95 \item \int_{-\infty}^{\infty} e^{-x^2} dx = \sqrt{\pi}
96 \end{block}
97 \end{frame}
98 \begin{frame}{Question 5}
99 \begin{block}
100
101 \item Positive numbers a, b, and c are the side
lengths of a triangle if and only if  $a + b > c$ ,  $b + c > a$ , and  $c + a > b$ .\\
102 \end{block}
103 \begin{block}
104
105 \item The area of a triangle with side lengths
a, b, and c is given by Heron's formula:
106 
$$A = \sqrt{s(s-a)(s-b)(s-c)}$$
, where s is the semiperimeter  $(a+b+c)/2$ .\\
107 \end{block}
108 \end{block}
109 \begin{block}
110
111 \item The volume of a regular tetrahedron of
edge length 1 is  $\sqrt{2}/12$ .\\
112 \end{block}
113 \end{frame}
114
115 \begin{frame}{Remaining Parts of Question 5}
116 \begin{block}
117
118 \item The quadratic equation  $ax^2 + bx + c = 0$  has
roots
119 
$$r_1, r_2 = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

120 \end{block}
121 \begin{block}
122
123 \item The derivative of a function f, denoted f', is
defined by
124 
$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

125 \end{block}
126 \begin{block}
127

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127
128      A real valued function  $f$  is convex on an
           interval  $I$  if
129       $\lambda f(\lambda x + (1-\lambda)y) \leq \lambda$ 
            $f(x) + (1-\lambda)f(y), \forall$  for all  $(x,y) \in$ 
            $I \times I$ ; and  $0 \leq \lambda \leq 1$ .
130  \end{block}
131  \end{frame}
132
133 \begin{frame}{Remaining Parts of Question 5}
134 \begin{block}
135
136      The general solution to the differential
           equation
137       $y'' - 3y' + 2y = 0$  is
138       $y = C_1 e^x + C_2 e^{2x}$ 
139  \end{block}
140 \begin{block}
141
142      The Fermat number  $F_n$  is defined as
143       $F_n = 2^{2^n}$ ,  $n \geq 0$ .
144  \end{block}
145 \end{frame}
146 \begin{frame}{Question 6}
147 \begin{block}
148
149       $\frac{d}{dx} \left( \frac{x}{x+1} \right) = \frac{1}{(x+1)^2}$ 
150  \end{block}
151 \begin{block}
152
153       $\lim_{n \rightarrow \infty} \left( 1 + \frac{1}{n} \right)^n = e$ 
154  \end{block}
155 \begin{block}
156
157      \begin{vmatrix}
158          a & b \\
159          c & d
160      \end{vmatrix} = ad - bc
161  \end{block}
162 \begin{block}
163

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163
164      \left[ \begin{array}{cc}
165          \cos \theta & -\sin \theta \\
166          \sin \theta & \cos \theta
167      \end{array} \right]
168
169  \right]
170
171 \end{block}
172 \end{frame}
173 \begin{frame}{Remaining Parts of Question 6}
174 \begin{block}
175
176 \item[\begin{vmatrix} \textbf{i} & \textbf{j} & \textbf{k} \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix}]
177 = \begin{vmatrix} a_2 & a_3 \\ b_2 & b_3 \end{vmatrix} \textbf{i} - \begin{vmatrix} a_1 & a_3 \\ b_1 & b_3 \end{vmatrix} \textbf{j} + \begin{vmatrix} a_1 & a_2 \\ b_1 & b_2 \end{vmatrix} \textbf{k}
178 \end{block}
179 \begin{block}
180
181 \item[\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}]
182 \end{bmatrix}
183 \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix} =
184 \begin{bmatrix} a_{11}b_{11} + a_{12}b_{12} & a_{11}b_{21} + a_{12}b_{22} \\ a_{21}b_{11} + a_{22}b_{12} & a_{21}b_{21} + a_{22}b_{22} \end{bmatrix}
185 \begin{bmatrix} a_{11}b_{11} + a_{12}b_{12} & a_{11}b_{21} + a_{12}b_{22} \\ a_{21}b_{11} + a_{22}b_{12} & a_{21}b_{21} + a_{22}b_{22} \end{bmatrix}
186 \end{bmatrix}
187 \begin{bmatrix} a_{11}b_{11} + a_{12}b_{12} & a_{11}b_{21} + a_{12}b_{22} \\ a_{21}b_{11} + a_{22}b_{12} & a_{21}b_{21} + a_{22}b_{22} \end{bmatrix}
188 \end{bmatrix}
189 \end{block}
190 \begin{block}
191
192 \item  $f(x) = \begin{cases} -x^2, & x < 0 \\ x^2, & 0 \leq x \leq 2 \\ 4, & x > 2 \end{cases}$ 
193 \end{cases}
194
195
196 \end{cases}
197 \end{block}
198 \end{frame}
199 \begin{frame}{Question 7 Part 1}
200 \begin{block}
201

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202 - \begin{align*}
203     1+2 \quad &= \quad 3 \\
204     4+5+6 \quad &= \quad 7+8 \\
205     9+10+11+12 \quad &= \quad 13+14+15 \\
206     16+17+18+19+20 \quad &= \quad 21+22+23+24 \\
207     25+26+27+28+29+30 \quad &= \quad 31+32+33+34+35 \\
208 \end{align*}
209 \end{block}
210 \end{frame}
211 - \begin{frame}{Part 2}
212 - \begin{block}
213
214 - \begin{align*}
215     (a+b)^2 \quad &= \quad (a+b)(a+b) \\
216     &= \quad (a+b)a + (a+b)b \\
217     &= \quad a(a+b) + b(a+b) \\
218     &= \quad a^2+ab+\cancel{ba}+b^2 \\
219     &= \quad a^2+ab+ab+b^2 \\
220     &= \quad a^2+2ab+b^2 \\
221 \end{align*}
222 \end{block}
223 \end{frame}
224 - \begin{frame}{Part 3}
225 - \begin{block}
226
227 - \begin{align*}
228 \tan(\alpha+\beta+\gamma) &= \frac{\tan(\alpha+\beta)}{1-\tan(\alpha+\beta)\tan\gamma} \\
&= \frac{\frac{\tan\alpha+\tan\beta}{1-\tan\alpha\tan\beta}}{1-(\frac{\tan\alpha+\tan\beta}{1-\tan\alpha\tan\beta})\tan\gamma} \\
229 &= \frac{\tan\alpha+\tan\beta+(1-\tan\alpha\tan\beta)\tan\gamma}{1-\tan\alpha\tan\beta-(\tan\alpha+\tan\beta)\tan\gamma} \\
230 &= \frac{\tan\alpha+\tan\beta+\tan\gamma-\tan\alpha\tan\beta\tan\gamma}{1-\tan\alpha\tan\beta-\tan\alpha\tan\gamma-\tan\beta\tan\gamma} \\
231 &= \frac{\tan\alpha+\tan\beta+\tan\gamma-\tan\alpha\tan\beta\tan\gamma}{1-\tan\alpha\tan\beta-\tan\alpha\tan\gamma-\tan\beta\tan\gamma} \\
232 \end{align*}
233 \end{block}
234 \end{frame}
235 - \begin{frame}{Part 4}
236 - \begin{block}
237
238 - \begin{eqnarray*}
239 \prod_p \left(1 - \frac{1}{p^2}\right) &= \prod_p \frac{1}{1 + \frac{1}{p^2} + \frac{1}{p^4} + \cdots} \\
240 &= \left(\prod_p \left(1 + \frac{1}{p^2} + \frac{1}{p^4} + \cdots\right)\right)^{-1}
\end{eqnarray*}

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240 &=& \left( \prod_p \left( 1 + \frac{1}{p^2} + \frac{1}{p^4} + \dots \right) \right)^{-1} \\
241 &=& \left( 1 + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots \right)^{-1} \\
242 &=& \frac{6}{\pi^2} \\
243 \end{eqnarray*} \\
244 \end{block} \\
245 \end{frame} \\
246 \setbeamertemplate{background}{\includegraphics[width=\paperwidth,height=\paperheight]{thankyou.jpg}} \\
247 \begin{frame} \\
248 \\
249 \end{frame} \\
250 \end{document}
```