

Beamer

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Let $x = (x_1, ..., x_n)$, where the x_i are non negative real numbers. Set

$$M_r(\mathsf{x}) = \left(\frac{\mathsf{x}_1^r + \mathsf{x}_2^r + \dots + \mathsf{x}_n^r}{n}\right)^{1/r}, \ \ r \in \mathsf{R} \setminus \{0\},$$

and

$$M_0(x) = (x_1 x_2 \dots x_n)^{1/n}$$

We call $M_r(x)$ the *rth power mean* of x Claim:

$$\lim_{r\to 0} M_r(x) = M_O(x)$$

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2 Define

$$V_{n} = \begin{bmatrix} 1 & 1 & 1 & \dots & 1 \\ x_{1} & x_{2} & x_{3} & \dots & x_{n} \\ x_{1}^{2} & x_{2}^{2} & x_{3}^{2} & \dots & x_{n}^{2} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ x_{1}^{n-1} & x_{2}^{n-1} & x_{3}^{n-1} & \dots & x_{n}^{n-1} \end{bmatrix}$$

We call V_n the Vandermonde matrix of order n Claim:

$$\det V_n = \prod_{1 \le i \le j \le n} (x_j - x_i)$$

Equations

$$3^3 + 4^3 + 5^3 = 6^3$$

$$\sqrt{100} = 10$$

$$(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$$

$$\sum_{k=1}^{n} k = \frac{n(n+1)}{2}$$

$$\frac{\pi}{4} = \frac{1}{1} - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \frac{1}{11} + \cdots$$

$$\cos\theta = \sin(90^\circ - \theta)$$

$$e^{i\theta} = \cos\theta + i\sin\theta$$

$$\lim_{\theta \to 0} \frac{\sin \theta}{\theta} = 1$$

$$\lim_{x \to \infty} \frac{\pi(x)}{x/\log x} = 1$$

$$\int_{-\infty}^{\infty} e^{-x^2} dx = \sqrt{\pi}$$

- Positive numbers a, b, and c are the side lengths of a triangle if and only if a + b > c, b + c > a, and c + a > b
- The area of a triangle with side lengths *a*, *b*, *c* is given by *Heron's formula*:

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

where s is the semiperimeter (a+b+c)/2.

- The volume of a regular tetrahedron of edge length 1 is $\sqrt{2}/12$.
- The quadratic equation $ax^2 + bx + c = 0$ has roots

$$r_1, r_2 = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

■ The derivative of a function f, denoted by f', is defined by

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

A real-valued function f is convex on an interval I if

$$f(\lambda x + (1 - \lambda)y) \le \lambda f(x) + (1 - \lambda)f(y)$$

for all $x, y \in I$ and $0 < \lambda < 1$

■ The general solution to the differential equation

$$y^n - 3y' + 2y = 0$$

is

$$y = C_1 e^x + C_2 e^{2x}$$

■ The Fermatnumber F_n is defined as

$$F_n = 2^{2^n}, n \ge 0$$

Make the following equation. Notice the large delimiters

$$\frac{d}{dx}\left(\frac{x}{x+1}\right) = \frac{1}{(x+1)^2}$$

$$\lim_{n\to\infty} (1+\frac{1}{n})^n = e$$

$$\left|\begin{array}{cc} a & b \\ c & d \end{array}\right| = ad - bc$$

$$R_{\theta} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

$$\begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix} = \begin{vmatrix} a_2 & a_3 \\ b_2 & b_3 \end{vmatrix} \mathbf{i} - \begin{vmatrix} a_1 & a_3 \\ b_1 & b_3 \end{vmatrix} \mathbf{j} + \begin{vmatrix} a_1 & a_2 \\ b_1 & b_2 \end{vmatrix} \mathbf{k}$$

Make the following equation. Notice the large delimiters

$$\left[\begin{array}{cc} a_{11} & a_{12} \\ a_{21} & a_{22} \end{array}\right] \left[\begin{array}{cc} b_{11} & b_{12} \\ b_{21} & b_{22} \end{array}\right] = \left[\begin{array}{cc} a_{11}b_{11} + a_{12}b_{21} & a_{11}b_{12} + a_{12}b_{22} \\ a_{21}b_{11} + a_{22}b_{21} & a_{21}b_{12} + a_{22}b_{22} \end{array}\right]$$

$$f(x) = \begin{cases} -x^2 & x < 0 \\ x^2, & 0 \le x \le 2 \\ 4, & x > 2 \end{cases}$$

$$1+2 = 3$$

$$4+5+6 = 7+8$$

$$9+10+11+12 = 13+14+15$$

$$16+17+18+19+20 = 21+22+23+24$$

$$25+26+27+28+29+30 = 31+32+33+34+35$$

$$(a+b)^{2} = (a+b)(a+b)$$

$$= (a+b)a + (a+b)b$$

$$= a(a+b) + b(a+b)$$

$$= a^{2} + ab + ba + b^{2}$$

$$= a^{2} + 2ab + b^{2}$$

$$= a^{2} + 2ab + b^{2}$$

$$\begin{split} \tan(\alpha+\beta+\gamma) &= \frac{\tan(\alpha+\beta)+\tan\gamma}{1-\tan(\alpha+\beta)\tan\gamma} \\ &= \frac{\frac{\tan\alpha+\tan\beta}{1-\tan\alpha\tan\beta}+\tan\gamma}{1-\frac{\tan\alpha+\tan\beta}{1-\tan\alpha\tan\beta}\tan\gamma} \\ &= \frac{\tan\alpha+\tan\beta}{1-\tan\alpha\tan\beta}\tan\gamma \\ &= \frac{\tan\alpha+\tan\beta+(1-\tan\alpha\tan\beta)\tan\gamma}{1-\tan\alpha\tan\beta-(\tan\alpha+\tan\beta)\tan\gamma} \\ &= \frac{\tan\alpha+\tan\beta+\tan\gamma-\tan\alpha\tan\beta\tan\gamma}{1-\tan\alpha\tan\beta-\tan\alpha\tan\gamma-\tan\beta\tan\gamma} \end{split}$$

$$\prod_{p} \left(1 - \frac{1}{p^2} \right) = \prod_{p} \frac{1}{1 + \frac{1}{p^2} + \frac{1}{p^4} + \cdots}$$

$$= \left(\prod_{p} \left(1 + \frac{1}{p^2} + \frac{1}{p^4} + \cdots \right) \right)^{-1}$$

$$= \left(1 + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} \cdots \right)^{-1}$$

$$= \frac{6}{\pi^2}$$

