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1 \documentclass{beamer}
2 \usepackage[utf8]{inputenc}
3 \usepackage{kerkis}
4 \usepackage{tcolorbox}
5
6 \title{ASSIGNMENT 2}
7 \subtitle{\LaTeX Presentation}
8 \author{Ritika Kamboj \\ MAT/20/122\\ 20044563047}
9 \date{}
10 \institute{Mata Sundri College For Women \\University of Delhi}
11
12 \usetheme[Berlin]
13   \usecolortheme{beaver}
14   \usefonttheme{serif}
15
16
17 \begin{document}
18 {\setbeamertemplate{background}{\includegraphics[width=\paperwidth,height=\paperheight]{background.jpeg}}}
19 \begin{frame}
20   \titlepage
21
22 \end{frame}
23 \begin{frame}
24   \frametitle{Content of the page number 69}
25 \begin{enumerate}
26   \item
27     Let  $\mathbf{x} = \{x_1, \dots, x_n\}$ , where the  $x_i$  are non-negative real numbers.
28     Set
29      $M_r(\mathbf{x}) = \left( \frac{x_1^r + x_2^r + \dots + x_n^r}{n} \right)^{1/r}$ ,
30      $r \in \mathbf{R} \setminus \{0\}$ ,
31     and
32      $M_0(\mathbf{x}) = \left( x_1 x_2 \cdots x_n \right)^{1/n}$ .
33     We call  $M_r(\mathbf{x})$  the  $r^{\text{th}}$  power mean of  $\mathbf{x}$ . //
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33 We call  $M_r(\mathbf{x})$  the  $\text{em}\{r^{\text{th}}$  power mean} of  $\mathbf{x}$ . \\
34 Claim:\\
35  $\lim_{r \rightarrow 0} M_r(\mathbf{x}) = M_0(\mathbf{x})$ .\\
36 \item\\
37 Define\\
38 \end{enumerate}\\
39 \end{frame}\\
40 \begin{frame}\\
41 \textcolor{red}{\boxed{V_n=}}\\
42 \quad \left[ \begin{array}{cccccc} \textcolor{brown}{\overbrace{\phantom{111111}}^{n \text{ rows}}} \\ | & 1 & 1 & 1 & \cdots & 1 \\ | & x_1 & x_2 & x_3 & \cdots & x_n \\ | & x_1^2 & x_2^2 & x_3^2 & \cdots & x_n^2 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ | & x_1^{n-1} & x_2^{n-1} & x_3^{n-1} & \cdots & x_n^{n-1} \end{array} \right] \\ \\
43 \quad \text{We call } \textcolor{blue}{V_n} \text{ the } \text{emph}{Vandermonde matrix} \text{ of order } n.\\
44 \quad \text{Claim: } \boxed{\det V_n = \prod_{1 \leq i < j \leq n} (x_j - x_i)}\\
45 \end{frame}\\
46 \begin{frame}\\
47 \text{Question. 4}\\
48 \begin{itemize}\\
49 \begin{tcolorbox}
50 \item  $3^3 + 4^3 + 5^3 = 6^3$  \\
51 \item  $\sqrt{100} = 10$  \\
52 \item  $(a+b)^3 = a^3 + b^3 + 3ab^2 + 3a^2b$  \\
53 \item  $\sum_{k=1}^n k = \frac{n(n+1)}{2}$  \\
54 \item  $\frac{\pi}{4} = \frac{1}{1} - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \frac{1}{11} + \dots$ 
55 \end{itemize}
56 \end{frame}\\
57 \begin{frame}\\
58 \text{Remaining parts of Ques.4}\\
59 \begin{itemize}
60 \item  $\frac{\pi}{4} = \frac{1}{1} - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \frac{1}{11} + \dots$ 
61 \end{itemize}
62 \end{frame}\\
63 \begin{frame}\\
64 \text{Remaining parts of Ques.4}\\
65 \begin{itemize}
66 \end{itemize}
67 \end{frame}

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64 \begin{frame}{Remaining parts of Ques.4}
65 \begin{itemize}
66   \item  $\cos\theta = \sin(90^\circ - \theta)$ 
67   \item  $e^{i\theta} = \cos\theta + i\sin\theta$ 
68   \item  $\lim_{x \rightarrow \infty} \frac{\sin\theta}{\theta} = 1$ 
69   \item  $\lim_{x \rightarrow \infty} \frac{\pi(x)}{x \log x} = 1$ 
70   \item  $\int_{-\infty}^{\infty} e^{-x^2} dx = \sqrt{\pi}$ 
71 \end{itemize}
72 \end{frame}
73 \begin{frame}{Question 5}
74 \begin{itemize}
75   \item Positive numbers  $a, b$  and  $c$  are the side lengths of a triangle if and only if  $a+b > c, b+c > a$ , and  $c+a > b$ .
76   \item The area of a triangle with side lengths  $a, b, c$  is given by Heron's formula:
77   
$$A = \sqrt{s(s-a)(s-b)(s-c)},$$

78   where  $s$  is the semiperimeter  $(a+b+c)/2$ .
79   \item The volume of a regular tetrahedron of edge length 1 is  $\sqrt{2}/12$ .
80   \item The quadratic equation  $ax^2+bx+c=0$  has roots  $r_1, r_2 = \frac{-b \pm \sqrt{b^2-4ac}}{2a}$ .
81 \end{itemize}
82 \end{frame}
83 \begin{frame}{Remaining Parts of Ques.5}
84 \begin{itemize}
85   \item The derivative of a function  $f$ , denoted  $f'$ , is defined by  $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h)-f(x)}{h}$ .
86   \item A real-valued function  $f$  is convex on an interval  $I$  if  $f(\lambda x + (1-\lambda)y) \leq \lambda f(x) + (1-\lambda)f(y)$ , for all  $x, y \in I$ ; and  $0 \leq \lambda \leq 1$ 
87   \item The general solution to the differential equation  $y'' - 3y' + 2y = 0$  is  $y = C_1 e^x + C_2 e^{2x}$ .
88 \end{itemize}
89 \end{frame}
90 \begin{frame}{Remaining part of Ques.5}
91 \begin{itemize}
92   \item The Fermat number  $F_n$  is defined as  $F_n = 2^{2^n}, n \geq 0$ .
93 \end{itemize}
94 \end{frame}
95 \end{frame}
96 \end{frame}

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96 \end{frame}
97 \begin{frame}{Question 6}
98 \begin{itemize}
99   \item  $\frac{d}{dx} \left( \frac{x}{x+1} \right) = \frac{1}{(x+1)^2}$ 
100  \item  $\lim_{n \rightarrow \infty} \left( 1 + \frac{1}{n} \right)^n = e$ 
101  \item  $\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$ 
102  \item  $R_\theta = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix}$ 
103 \end{itemize}
104 \end{frame}
105 \begin{frame}{Remaining Parts of Ques.6}
106 \begin{itemize}
107   \item  $\begin{vmatrix} i & j & k \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix} = \begin{vmatrix} a_2 & a_3 \\ b_2 & b_3 \end{vmatrix}$ 
108   \item  $i - \begin{vmatrix} a_1 & a_3 \\ b_1 & b_3 \end{vmatrix}$ 
109   \item  $\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix} = \begin{bmatrix} a_{11}b_{11} + a_{12}b_{21} & a_{11}b_{12} + a_{12}b_{22} \\ a_{21}b_{11} + a_{22}b_{21} & a_{21}b_{12} + a_{22}b_{22} \end{bmatrix}$ 
110   \item  $f(x) = \begin{cases} -x^2, & x < 0 \\ x^2, & 0 \leq x \leq 2 \\ 4, & x > 2 \end{cases}$ 
111 \end{itemize}
112 \end{frame}
113 \begin{frame}{Question 7(1)}
114 \begin{align*}
115   & 1+2 &= 3 \\
116   & 4+5+6 &= 7+8 \\
117   & 9+10+11+12 &= 13+14+15 \\
118   & 16+17+18+19+20 &= 21+22+23+24 \\
119   & 25+26+27+28+29+30 &= 31+32+33+34+35
120 \end{align*}
121 \end{frame}
122 \begin{frame}{Question 7(2)}
123 \begin{align*}
124 \end{align*}
125 \end{frame}
126 \begin{frame}{Question 7(2)}
127 \begin{align*}
128 \end{align*}
129 \end{frame}
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125 \begin{frame}{Question 7(2)}
126   \begin{align*}
127     (a+b)^2 &= (a+b)(a+b) \\
128     &= (a+b)a + (a+b)b \\
129     &= a(a+b) + b(a+b) \\
130     &= a^2 + ab + ba + b^2 \\
131     &= a^2 + ab + ab + b^2 \\
132     &= a^2 + 2ab + b^2
133   \end{align*}
134 \end{frame}
135 \begin{frame}{Question 7(3)}
136   \begin{align*}
137     \tan(\alpha+\beta+\gamma) &= \frac{\tan(\alpha+\beta)+\tan\gamma}{1-\tan(\alpha+\beta)\tan\gamma} \\
138     &\equiv \frac{\frac{\tan\alpha+\tan\beta}{1-\tan\alpha\tan\beta}+\tan\gamma}{1-\left(\frac{\tan\alpha+\tan\beta}{1-\tan\alpha\tan\beta}\right)\tan\gamma} \\
139     &\equiv \frac{\tan\alpha+\tan\beta+(1-\tan\alpha\tan\beta)\tan\gamma}{1-\tan\alpha\tan\beta-(\tan\alpha+\tan\beta)\tan\gamma} \\
140     &\equiv \frac{\tan\alpha+\tan\beta+\tan\gamma-\tan\alpha\tan\beta\tan\gamma}{1-\tan\alpha\tan\beta-\tan\alpha\tan\gamma-\tan\beta\tan\gamma}
141   \end{align*}
142 \end{frame}
143 \begin{frame}{Question 7(4)}
144   \begin{align*}
145     \prod_p (1 - \frac{1}{p^2}) &= \prod_p \frac{1 + \frac{1}{p^2} + \frac{1}{p^4} + \dots}{1 - \frac{1}{p^2}} \\
146     &\equiv \left( \prod_p \left( 1 + \frac{1}{p^2} + \frac{1}{p^4} + \dots \right) \right)^{-1} \\
147     &\equiv \left( 1 + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots \right)^{-1} \\
148     &\equiv \frac{6}{\pi^2}
149   \end{align*}
150 \end{frame}
151 \setbeamertemplate{background}{\includegraphics[width=\paperwidth,height=\paperheight]{images.jpg}}
152 \begin{frame}
153
154 \end{frame}
155 \end{document}
156
157

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