

PRACTICAL 1

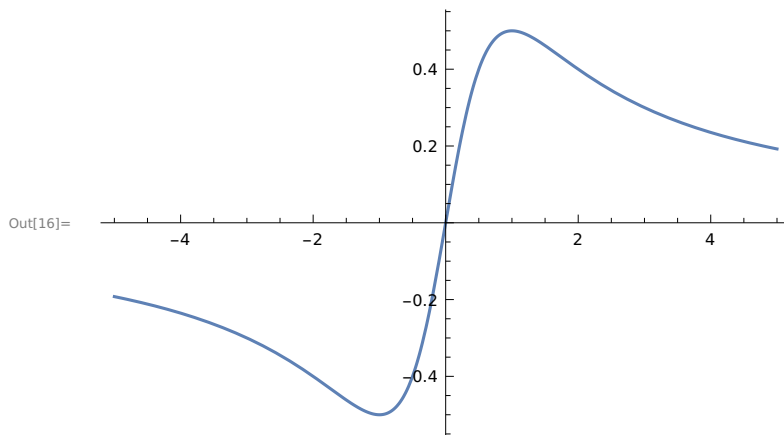
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Q1. Graph each of the following functions.

a) $f(x)=x/(1+x^2)$

```
In[15]:= f[x_] :=  $\frac{x}{1+x^2}$ ;
```

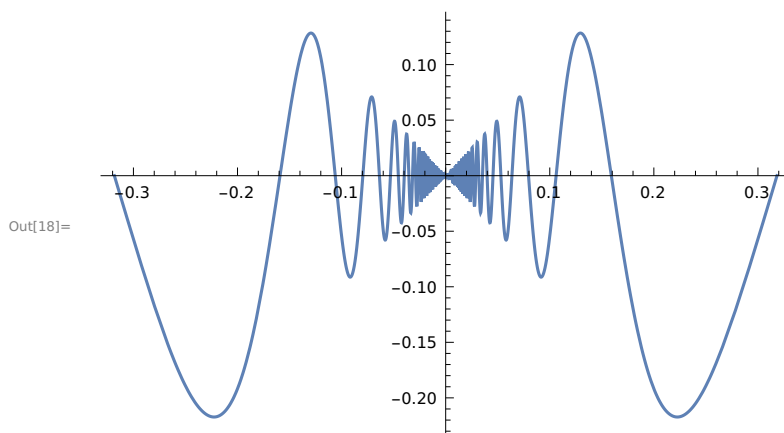
```
In[16]:= Plot[f[x], {x, 5, -5}]
```



b) $y=x \sin(1/x)$

```
In[17]:= y[x_] := x Sin (1 / x);
```

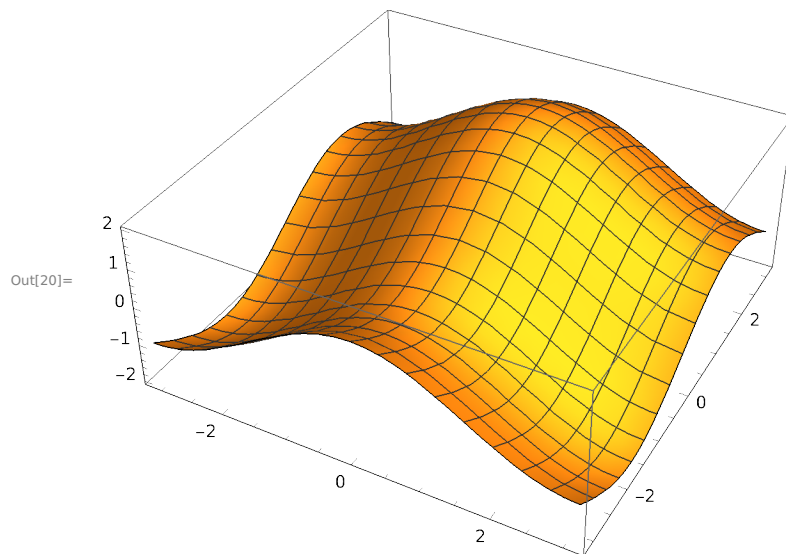
```
Plot[x Sin[1 / x], {x, 1 /  $\pi$ , -1 /  $\pi$ }]
```



```
In[19]:=
```

c) $g(x,y)=\cos(x)+\sin(y)$

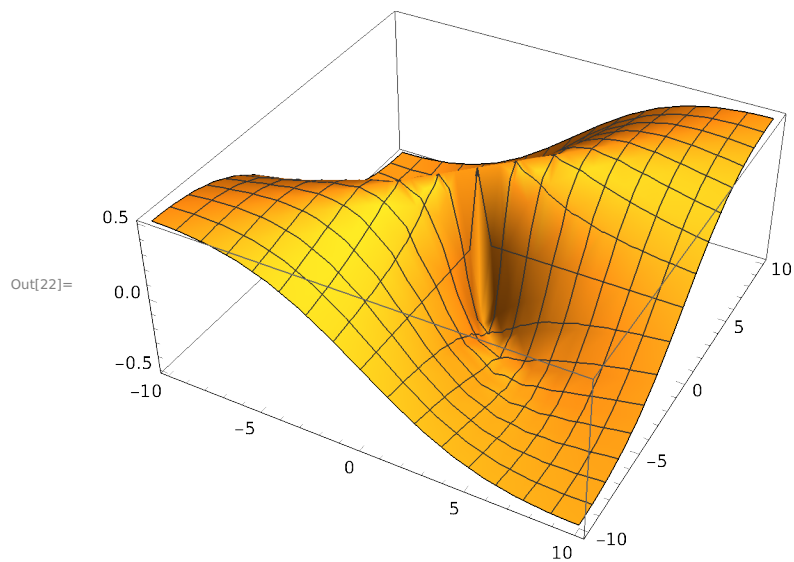
In[20]:= `Plot3D[Cos[x]+Sin[y], {x,  $\pi$ ,  $-\pi$ }, {y,  $\pi$ ,  $-\pi$ }]`



In[21]:= **(d)** $z = \frac{xy}{x^2 + y^2}$

Out[21]= $\frac{xy}{x^2 + y^2}$

In[22]:= `Plot3D[ $\frac{xy}{x^2 + y^2}$ , {x, 10, -10}, {y, 10, -10}]`



Q2. Let $f[x_] := x / (1 + x^2)$

(a) $f'[x]$

Out[24]= $-\frac{2x^2}{(1+x^2)^2} + \frac{1}{1+x^2}$

```
In[25]:= f''[x]
Out[25]= 
$$\frac{8x^3}{(1+x^2)^3} - \frac{6x}{(1+x^2)^2}$$

```

b) Find f'(-1) and f'(0)

```
In[26]:= f'[-1]
Out[26]= 0
```

```
In[27]:= f'[0]
Out[27]= 1
```

c) Find f''(0) and f''(1)

```
In[28]:= f''[0]
Out[28]= 0
```

```
In[29]:= f''[1]
Out[29]= 
$$-\frac{1}{2}$$

```

Q3). Find the prime factorization of each integer.

a) 3527218133309949276293

```
In[30]:= FactorInteger [ 3 527 218 133 309 949 276 293 ]
Out[30]= {{15 013 , 2}, {25 013 , 3}}
```

(b) 471945325930166269

```
In[31]:= FactorInteger [ 471 945 325 930 166 269 ]
Out[31]= {{4211 , 1}, {34 589 , 1}, {46 747 , 1}, {69 313 , 1}}
```

(c) 471945325930166281

```
In[32]:= FactorInteger [ 471 945 325 930 166 281 ]
Out[32]= {{471 945 325 930 166 281 , 1}}
```

Q4. Compute each expression. Do you notice a pattern?

(a) 3^6 mod 7

```
In[33]:= PowerMod [3, 6, 7]
Out[33]= 1
```

(b) 6^10 mod 11

```
In[34]:= PowerMod [6, 10, 11]
Out[34]= 1
```

(c) 7^20 mod 21

In[35]:= **PowerMod**[7, 20, 21]

Out[35]= 7

(d) $7^{22} \bmod 23$

In[36]:= **PowerMod**[7, 22, 23]

Out[36]= 1

Q8. Let $M = \{\{1, 1\}, \{0, 1\}\}$

(a) Find $M^2, M^3, \dots, M^{10}$.

In[37]:= **M** = **{{1, 1}, {1, 0}}**

Out[37]= **{{1, 1}, {1, 0}}**

In[38]:= **Table** [**MatrixPower** [**M**, **n**], {**n**, 2, 10}]

Out[38]= **{{{2, 1}, {1, 1}}, {{3, 2}, {2, 1}}, {{5, 3}, {3, 2}}, {{8, 5}, {5, 3}}, {{13, 8}, {8, 5}},
{{21, 13}, {13, 8}}, {{34, 21}, {21, 13}}, {{55, 34}, {34, 21}}, {{89, 55}, {55, 34}}}**

In[39]:= **Fibonacci** [100, **M**]

Out[39]= **{{354 224 848 179 261 915 075 , 354 224 848 179 261 915 075 }, {354 224 848 179 261 915 075 , 0}}**

In[40]:= **Fibonacci** [100]

Out[40]= 354 224 848 179 261 915 075

Q9. Find solutions to the following equations or systems of equations.

(a) Find x , if $x^2 + x = 1$.

In[41]:= **Solve**[$x^2 + x == 1$, **x**]

Out[41]= **{{ $x \rightarrow \frac{1}{2}(-1 - \sqrt{5})$ }, { $x \rightarrow \frac{1}{2}(-1 + \sqrt{5})$ }}**

(b) Find x , if $x^2 + x = -1$

In[42]:= **Solve**[$x^2 + x == -1$, **x**]

Out[42]= **{{ $x \rightarrow -(-1)^{1/3}$ }, { $x \rightarrow (-1)^{2/3}$ }}**

(c) Find x and y . $4x - 3y = 5$ and $6x + 2y = 14$

In[43]:= **Solve**[$4x - 3y == 5 \&\& 6x + 2y == 14$, {**x**, **y**}]

Out[43]= **{{ $x \rightarrow 2$, $y \rightarrow 1$ }}**

(d) Find x, y, z and t .

$-2x - 2y + 3z + t = 8$, $-3x + 0y - 6z + t = -19$, $6x - 8y + 6z + 5t = 47$, $x + 3y - 3z - t = -9$.

In[44]:= **Solve**[$-2x - 2y + 3z + t == 8 \&\&$

$-3x + 0y - 6z + t == -19 \&\& 6x - 8y + 6z + 5t == 47 \&\& x + 3y - 3z - t == -9$]

Out[44]= **{{ $t \rightarrow 5$, $x \rightarrow 2$, $y \rightarrow 1$, $z \rightarrow 3$ }}**

Q10. Solve this equation for r .

```
In[45]:= Solve[{250 e^r + 300 e^0.75 r + 350 e^0.5 r + 400 e^0.25 r == 1365}, r]
Out[45]:= {{r -> 0.541896}}
```

Q11. Write a function called mysqrt that accepts one argument, begins with an initial guess of 1.0, 0 finds 20 new guesses, and returns the answer.

```
In[46]:= mysqrt[n_] := Module[{i = 1, g = 1}, While[i ≤ 20, g =  $\frac{1}{2} \left( g + \frac{n}{g} \right)$ ; i = i + 1]; g]

In[47]:= N[mysqrt[2], 6]
Out[47]:= 1.41421

In[48]:= N[Sqrt[2], 6]
Out[48]:= 1.41421

In[49]:= N[mysqrt[3]]
Out[49]:= 1.73205
```

Q12. (a) Write a function called collatz that accepts a single argument, n, and returns:

- 0 if n=1,
- 1+collatz(n/2) if n is even.
- 1+collatz(3*n+1) if n is odd.

```
In[50]:= collatz[n_] := Which[n = 1, collatz[n] = 0, EvenQ[n],
    collatz[n] = 1 + collatz[n/2], OddQ[n], collatz[n] = 1 + collatz[3 * n + 1]];

In[50]:= collatz[1]
Out[50]:= 0

In[51]:= collatz[2]
Out[51]:= 1

In[52]:= collatz[6]
Out[52]:= 8

In[53]:= collatz[27]
Out[53]:= 111
```