

PRACTICAL 1

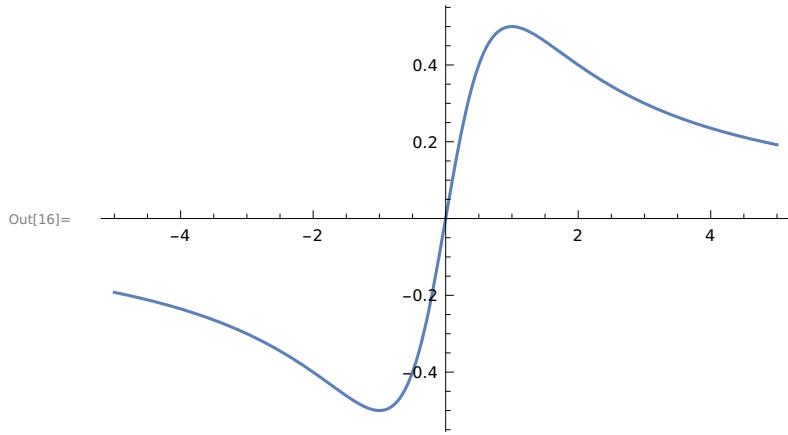
Priyanka Talwar. MAT/19/71

Q1. Graph each of the following functions.

a) $f(x)=x/(1+x^2)$

```
In[15]:= f[x_] := x / (1 + x^2);
```

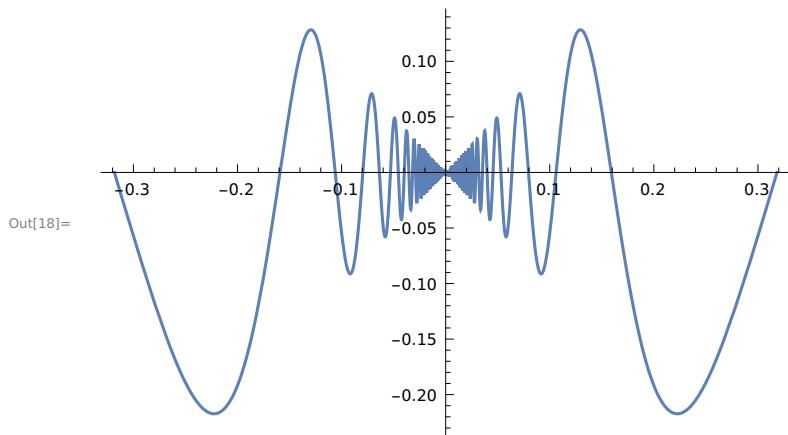
```
In[16]:= Plot[f[x], {x, -5, 5}]
```



b) $y=x \sin(1/x)$

```
In[17]:= y[x_] := x Sin(1/x);
```

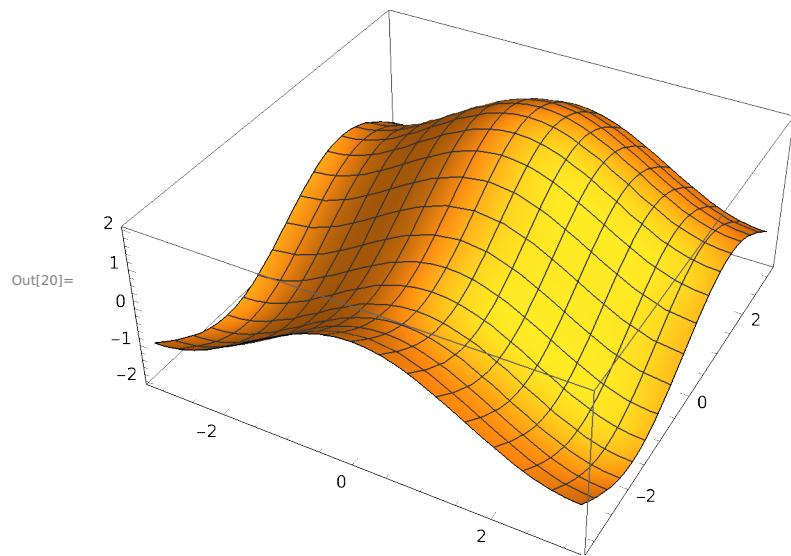
```
Plot[x Sin[1/x], {x, 1/\pi, -1/\pi}]
```



```
In[19]:=
```

c) $g(x,y)=\cos(x)+\sin(y)$

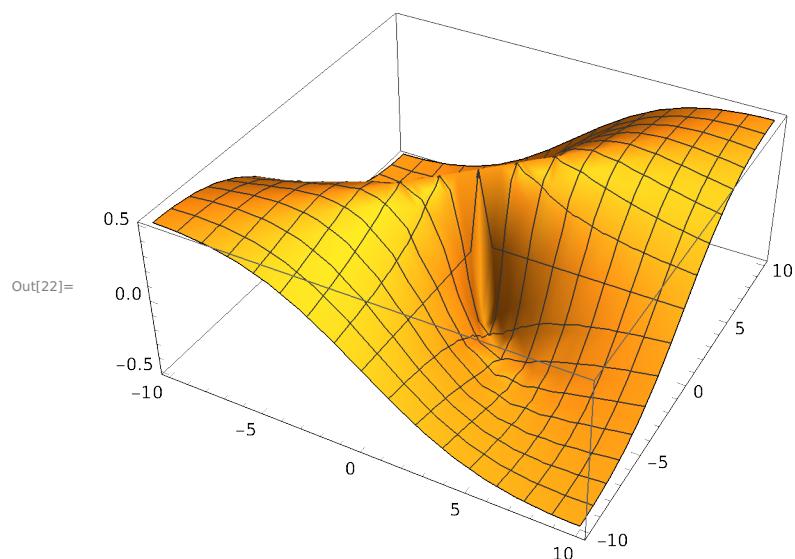
In[20]:= Plot3D[Cos[x] + Sin[y], {x, π, -π}, {y, π, -π}]



In[21]:= (d) $z = \frac{xy}{x^2 + y^2}$

Out[21]= $\frac{xy}{x^2 + y^2}$

In[22]:= Plot3D[$\frac{xy}{x^2 + y^2}$, {x, 10, -10}, {y, 10, -10}]



Q2. Let $f[x_] := x / (1 + x^2)$

(a) $f'[x]$

$$\text{Out[24]} = -\frac{2x^2}{(1+x^2)^2} + \frac{1}{1+x^2}$$

In[25]:= $f''[x]$

$$\text{Out[25]} = \frac{8x^3}{(1+x^2)^3} - \frac{6x}{(1+x^2)^2}$$

b) Find $f'(-1)$ and $f'(0)$

In[26]:= $f'[-1]$

$$\text{Out[26]} = 0$$

In[27]:= $f'[0]$

$$\text{Out[27]} = 1$$

c) Find $f''(0)$ and $f''(1)$

In[28]:= $f''[0]$

$$\text{Out[28]} = 0$$

In[29]:= $f''[1]$

$$\text{Out[29]} = -\frac{1}{2}$$

Q3). Find the prime factorization of each integer.

a) **3527218133309949276293**

In[30]:= **FactorInteger [3527218133309949276293]**

$$\text{Out[30]} = \{\{15013, 2\}, \{25013, 3\}\}$$

(b) **471945325930166269**

In[31]:= **FactorInteger [471945325930166269]**

$$\text{Out[31]} = \{\{4211, 1\}, \{34589, 1\}, \{46747, 1\}, \{69313, 1\}\}$$

(c) **471945325930166281**

In[32]:= **FactorInteger [471945325930166281]**

$$\text{Out[32]} = \{\{471945325930166281, 1\}\}$$

Q4. Compute each expression. Do you notice a pattern?

(a) **$3^6 \bmod 7$**

In[33]:= **PowerMod [3, 6, 7]**

$$\text{Out[33]} = 1$$

(b) $6^{10} \bmod 11$

```
In[34]:= PowerMod[6, 10, 11]
Out[34]= 1
```

(c) $7^{20} \bmod 21$

```
In[35]:= PowerMod[7, 20, 21]
Out[35]= 7
```

(d) $7^{22} \bmod 23$

```
In[36]:= PowerMod[7, 22, 23]
Out[36]= 1
```

Q8. Let $M = \begin{Bmatrix} 1 & 1 \\ 0 & 1 \end{Bmatrix}$ **(a) Find M^2, M^3, \dots, M^{10} .**

```
In[37]:= M = {{1, 1}, {0, 1}}
Out[37]= {{1, 1}, {0, 1}}
```

```
In[38]:= Table[MatrixPower[M, n], {n, 2, 10}]
```

```
Out[38]= {{{2, 1}, {1, 1}}, {{3, 2}, {2, 1}}, {{5, 3}, {3, 2}}, {{8, 5}, {5, 3}}, {{13, 8}, {8, 5}},
{{21, 13}, {13, 8}}, {{34, 21}, {21, 13}}, {{55, 34}, {34, 21}}, {{89, 55}, {55, 34}}}
```

```
In[39]:= Fibonacci[100, M]
```

```
Out[39]= {{354 224 848 179 261 915 075, 354 224 848 179 261 915 075}, {354 224 848 179 261 915 075, 0}}
```

```
In[40]:= Fibonacci[100]
```

```
Out[40]= 354 224 848 179 261 915 075
```

Q9. Find solutions to the following equations or systems of equations.**(a) Find x , if $x^2 + x = 1$.**

```
In[41]:= Solve[x^2 + x == 1, x]
Out[41]= {{x -> -1 - Sqrt[5]/2}, {x -> -1 + Sqrt[5]/2}}
```

(b) Find x , if $x^2 + x = -1$

```
In[42]:= Solve[x^2 + x == -1, x]
Out[42]= {{x -> -(-1)^{1/3}}, {x -> (-1)^{2/3}}}
```

(c) Find x and y . $4x - 3y = 5$ and $6x + 2y = 14$

```
In[43]:= Solve[4 x - 3 y == 5 && 6 x + 2 y == 14, {x, y}]
Out[43]= {{x -> 2, y -> 1}}
```

(d) Find x, y, z and t .

$-2x - 2y + 3z + t = 8$, $-3x + 0y - 6z + t = -19$, $6x - 8y + 6z + 5t = 47$, $x + 3y - 3z - t = -9$.

```
In[44]:= Solve[-2 x - 2 y + 3 z + t == 8 &&
           -3 x + 0 y - 6 z + t == -19 && 6 x - 8 y + 6 z + 5 t == 47 && x + 3 y - 3 z - t == -9]
Out[44]= {{t → 5, x → 2, y → 1, z → 3}}
```

Q10. Solve this equation for r.

```
In[45]:= Solve[{250 e^r + 300 e^0.75 r + 350 e^0.5 r + 400 e^0.25 r == 1365}, r]
Out[45]= {{r → 0.541896}}
```

Q11. Write a function called mysqrt that accepts one argument, begins with an initial guess of 1.0, finds 20 new guesses, and returns the answer.

```
In[46]:= mysqrt[n_] := Module[{i = 1, g = 1}, While[i ≤ 20, g =  $\frac{1}{2} \left( g + \frac{n}{g} \right)$ ; i = i + 1]; g]
```

```
In[47]:= N[mysqrt[2], 6]
Out[47]= 1.41421
```

```
In[48]:= N[Sqrt[2], 6]
Out[48]= 1.41421
```

```
In[49]:= N[mysqrt[3]]
Out[49]= 1.73205
```

Q12. (a) Write a function called collatz that accepts a single argument, n, and returns:

- 0 if n=1,
- 1+collatz(n/2) if n is even.
- 1+collatz(3*n+1) if n is odd.

```
In[50]:= collatz[n_] := Which[n = 1, collatz[n] = 0, EvenQ[n],
                           collatz[n] = 1 + collatz[n/2], OddQ[n], collatz[n] = 1 + collatz[3 * n + 1]];
```

```
In[50]:= collatz[1]
Out[50]= 0
```

```
In[51]:= collatz[2]
Out[51]= 1
```

```
In[52]:= collatz[6]
Out[52]= 8
```

```
In[53]:= collatz[27]
Out[53]= 111
```